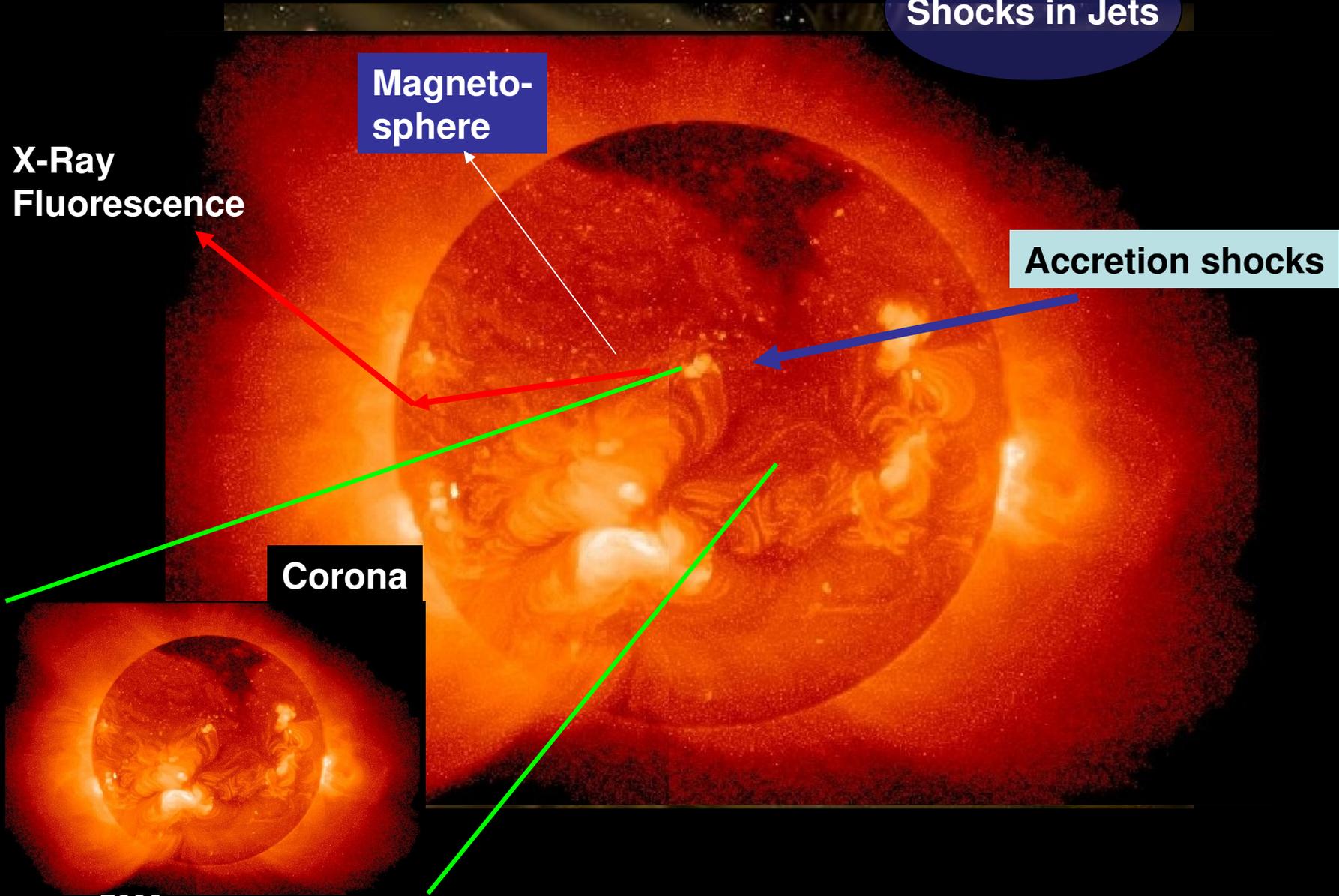


Stellar Coronae

Manuel Güdel

**Paul Scherrer Institut
Switzerland**

Shocks in Jets



The Sun:

$\approx 10^{27}$ erg/s in X-rays

$\approx 10^{-6} L_{\text{bol}}$

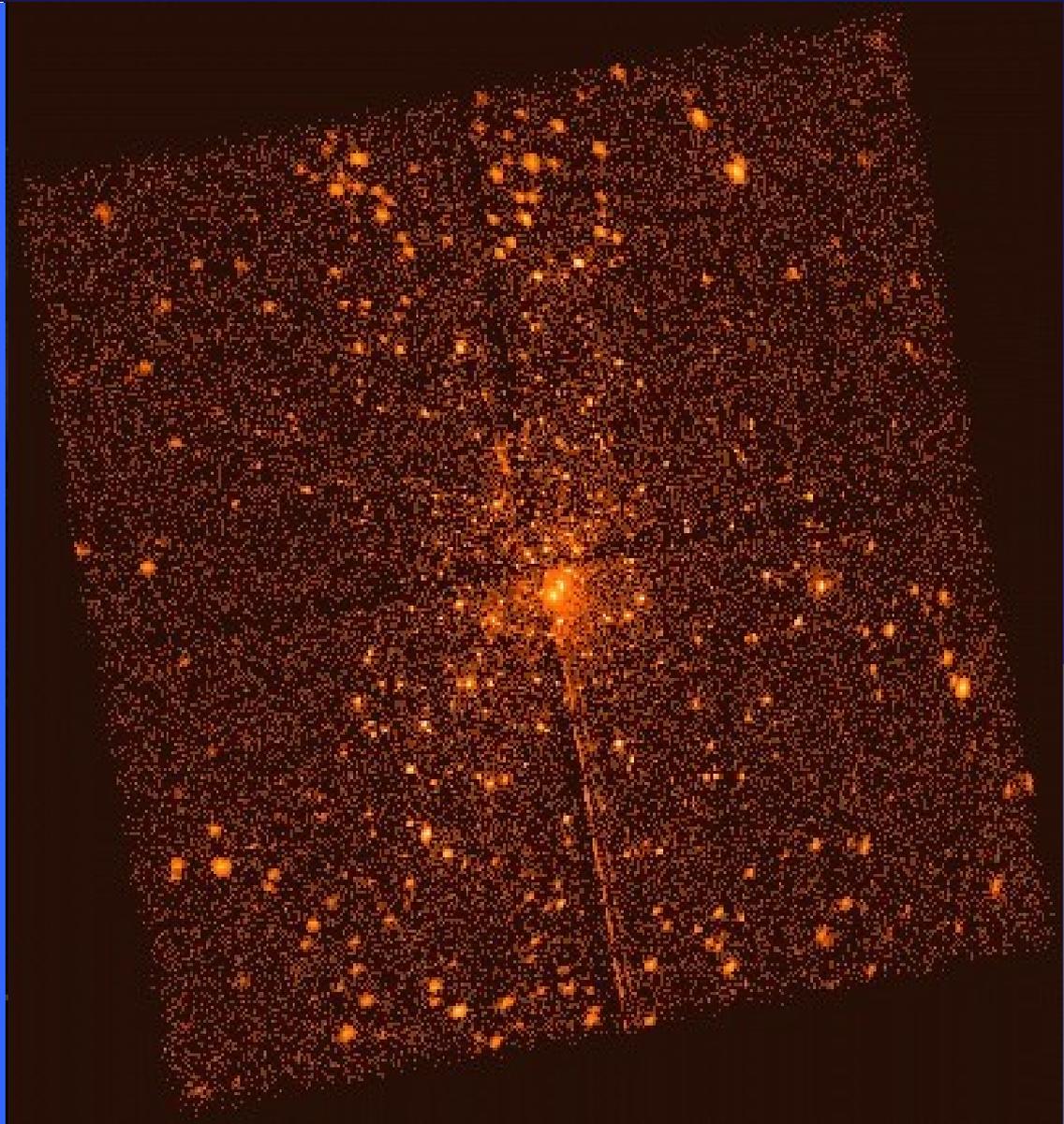


Orion Nebula Cluster

≈ 1500

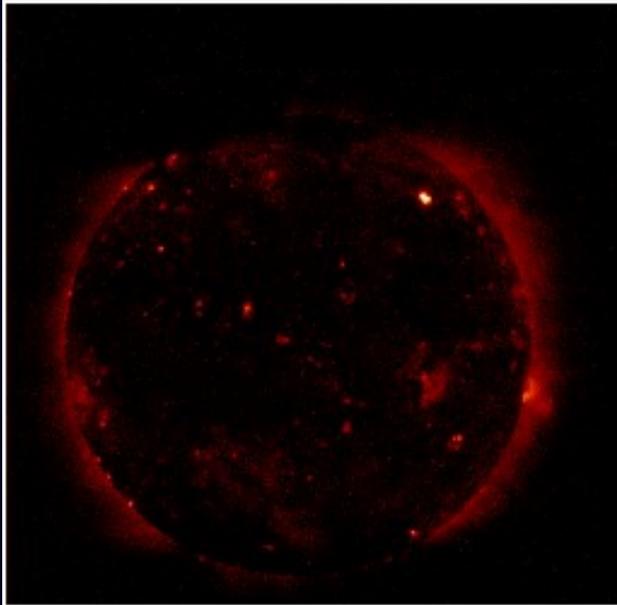
luminous X-ray stars

$\approx 10^{-3} L_{\text{bol}}$



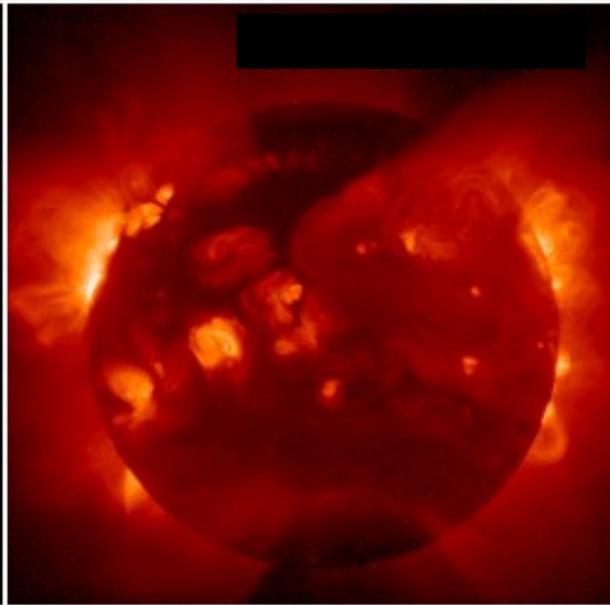
X-RAY PROBLEM:

THE X-RAY LUMINOSITY



minimum Sun

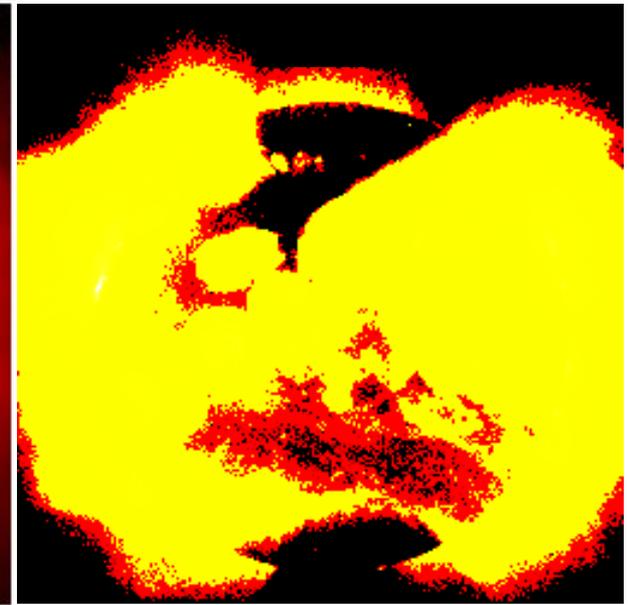
5×10^{26}



maximum Sun

5×10^{27}

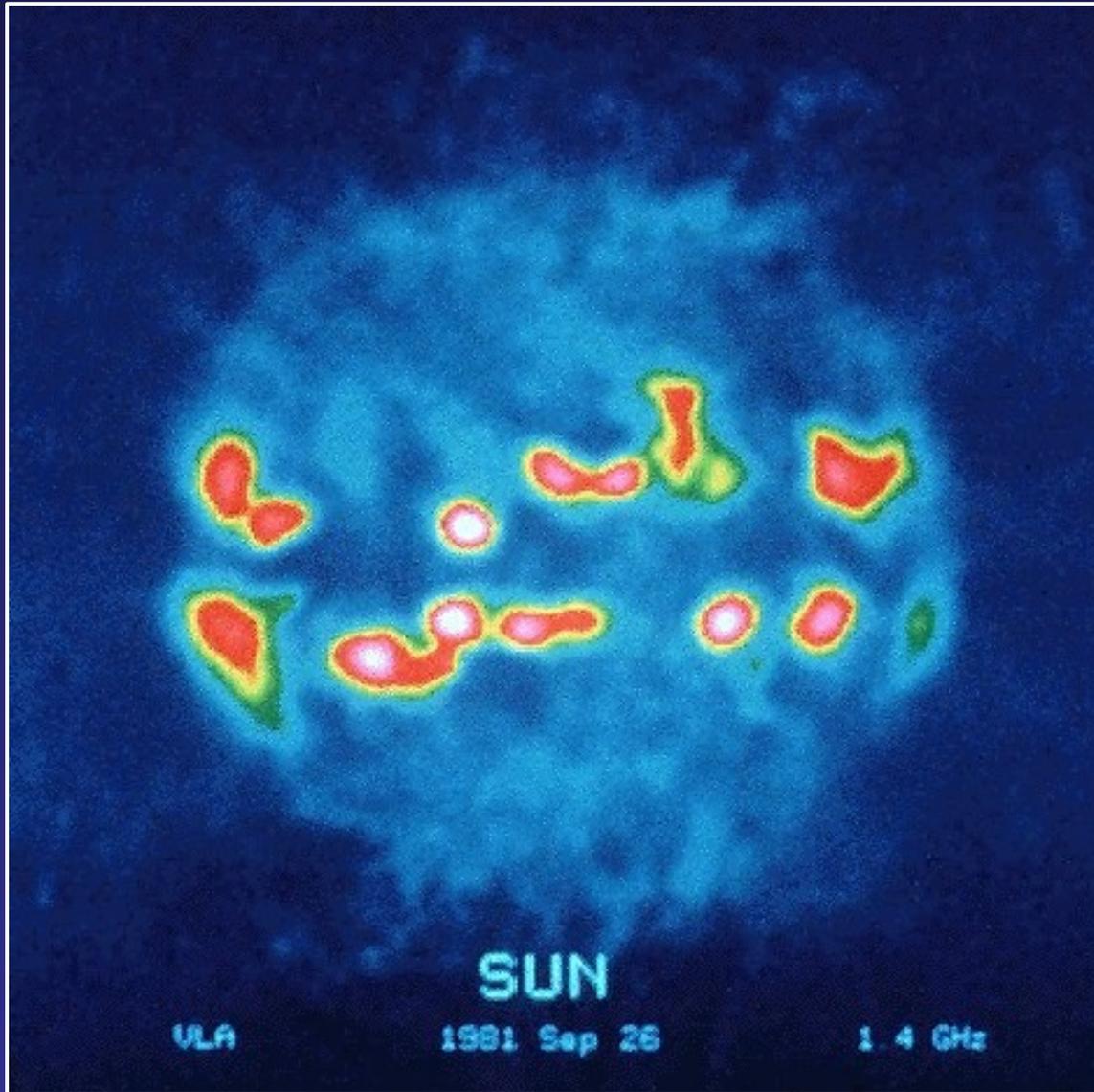
(ergs/s)



active star

3×10^{29}

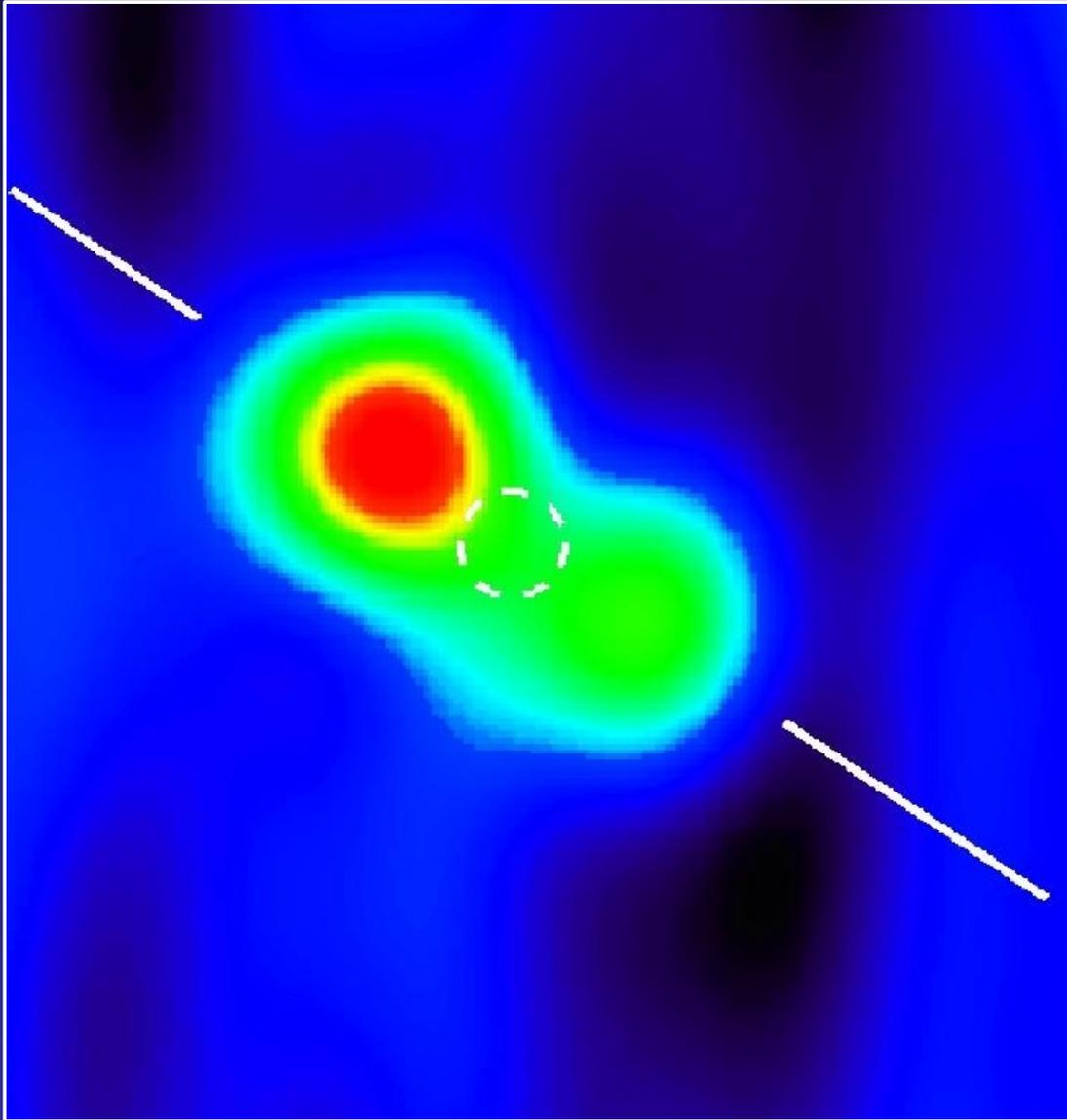
BUT: The most active solar analogs show 3×10^{30} !



The Radio Sun:

$$\approx (6-10) \times 10^{10} \text{ erg/s/Hz}$$

10 kK bremsstrahlung
&
1 MK cyclotron



The Radio UV Cet:

$$\approx 2 \times 10^{13} \text{ erg/s/Hz}$$

large source!

(Benz et al. 1998)

Outline

Coronal Structure

Coronal Spectroscopy

Fine Structure: Coronal Magnetic Loops

Coronal Flares

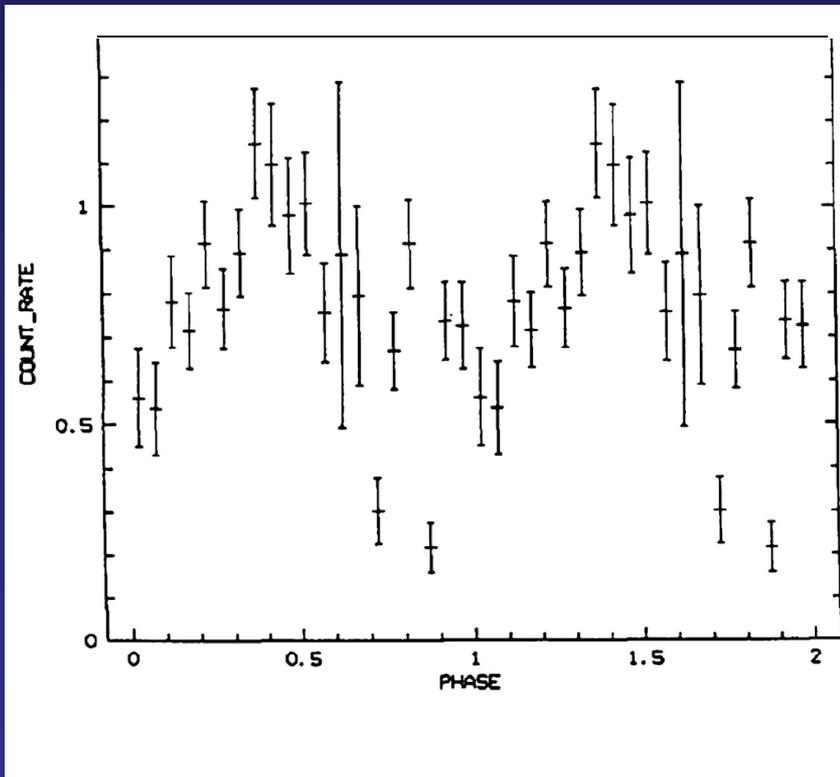
Continuous Flaring

Toward young, forming stars

Coronal Structure

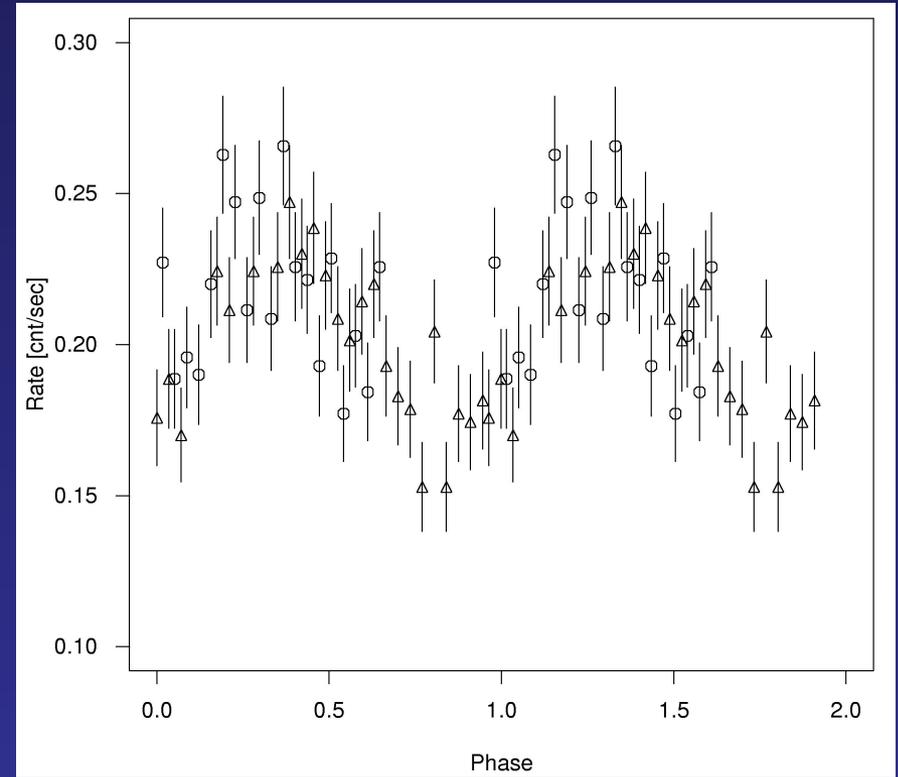
Coronal Imaging in X-rays

Principle: Use rotational self-eclipse of star or mutual eclipses in binaries to map structure



Cargese, 6 April
2006

(Güdel et al. 1995)



(Marino et al. 2003)

Coronal Imaging in X-rays

Principle: Use rotational self-eclipse of star or mutual eclipses in binaries to map structure

$$\frac{V_{\max}}{R_*^3} = \frac{\psi}{3} - \frac{(2\pi - \varphi)(1 + \sin^2 i)}{6\sin i} + \frac{2\cot(\chi/2)}{3\tan i}$$

$$\tan\chi = \tan(\varphi/2)\cos i$$

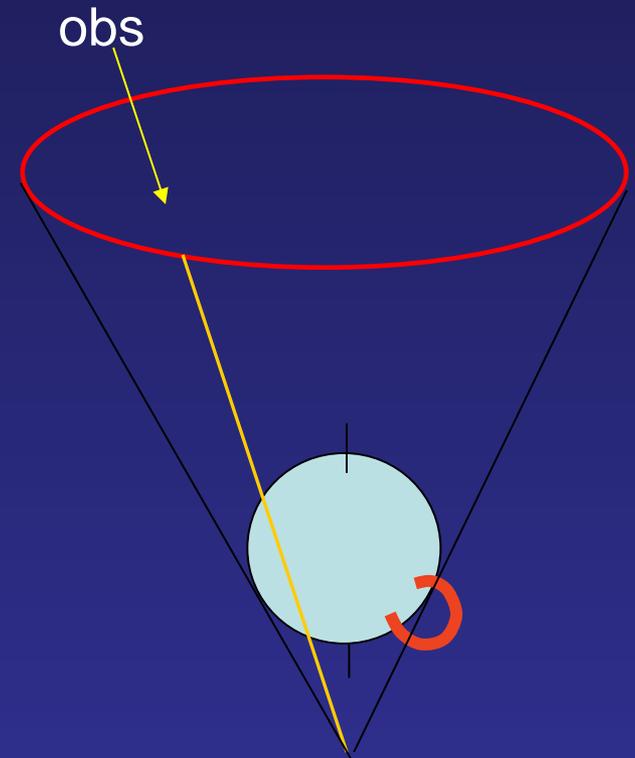
$$\sin(\psi/2) = \sin(\varphi/2)\sin i$$

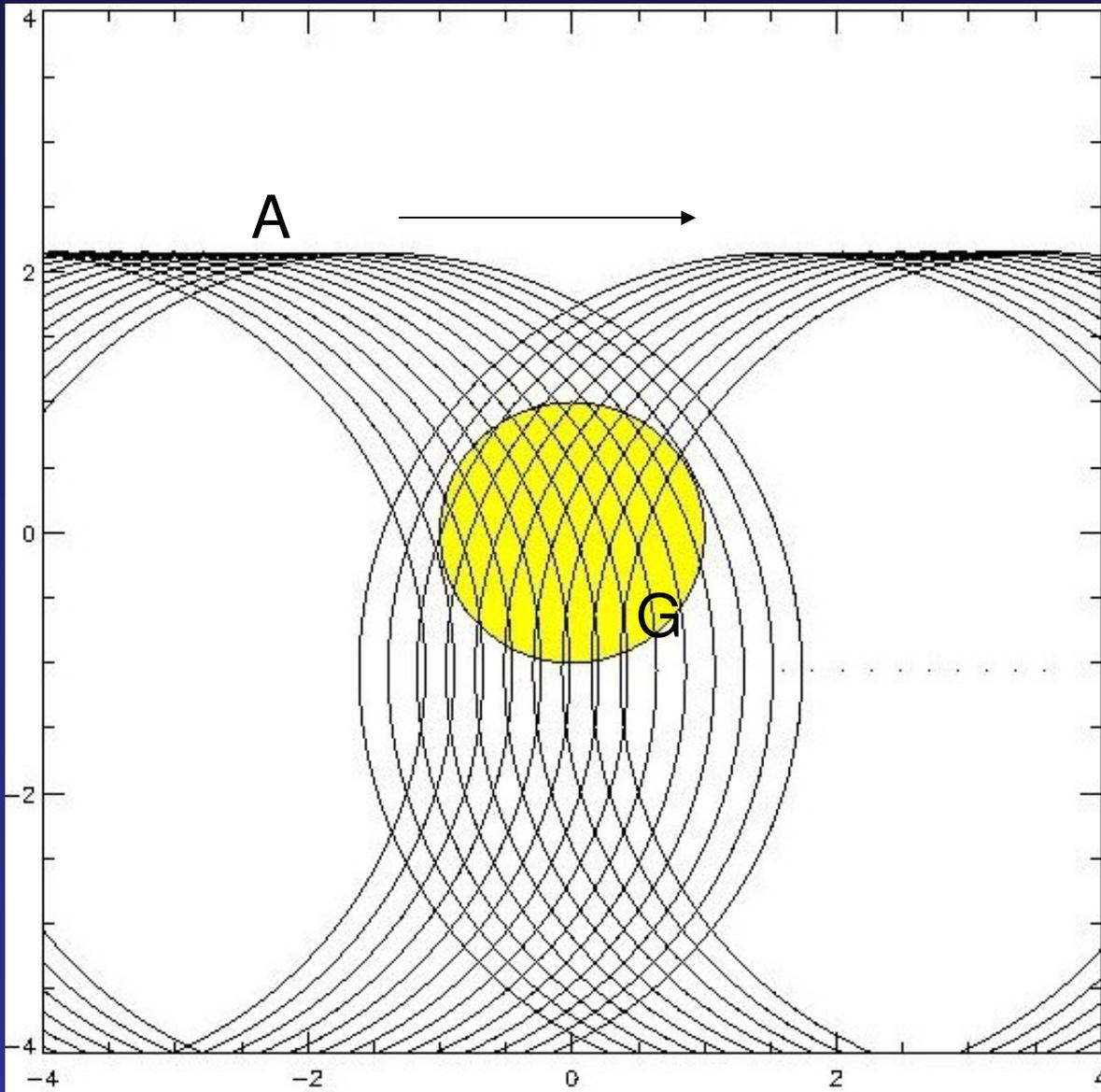
$$0 \leq \psi/2 \leq \pi/2$$

$\chi, \varphi/2$ in same quadrant

$$0 \leq i \leq \pi/2$$

(Güdel & Schmitt 1995)

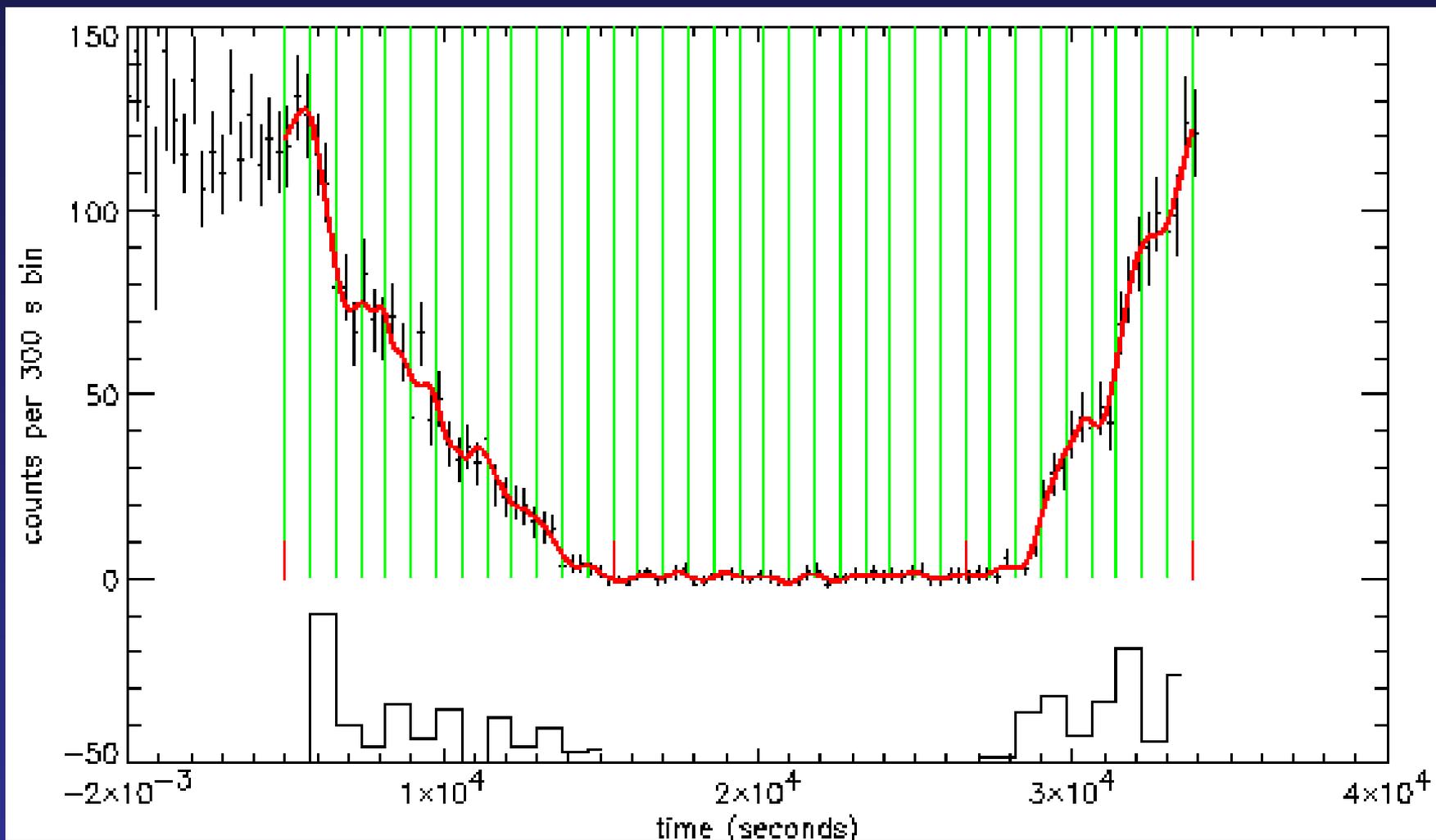


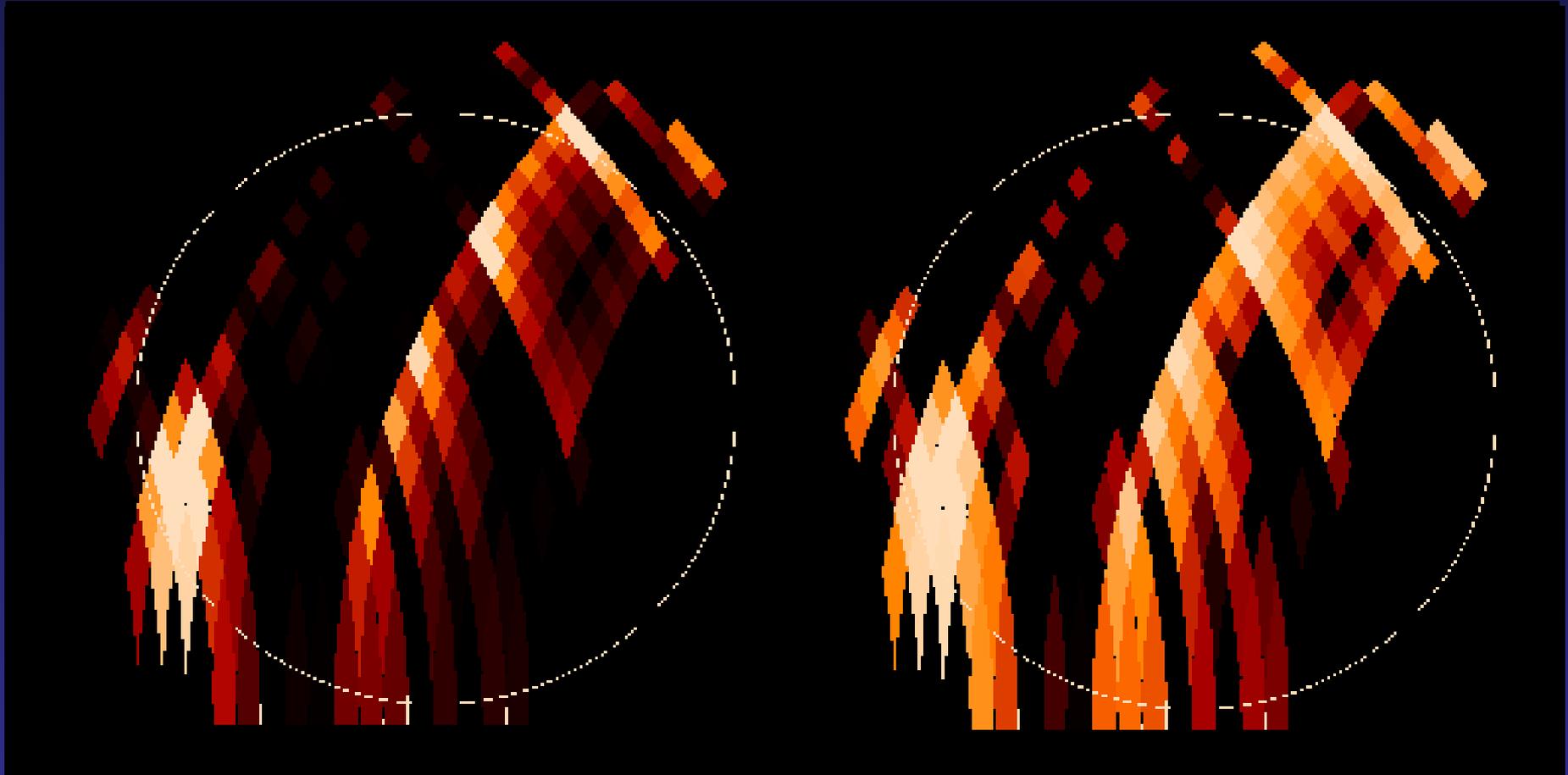


Monitor
eclipsing binary
system

Assume coronal star
at rest, eclipsing
star moving.

Limbs cut off slices
from coronal star

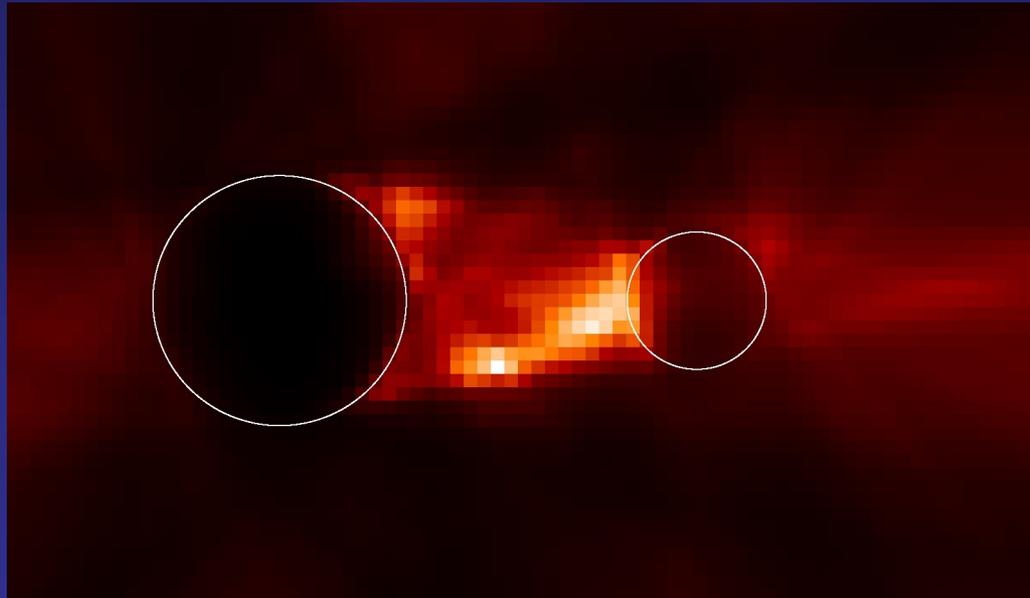
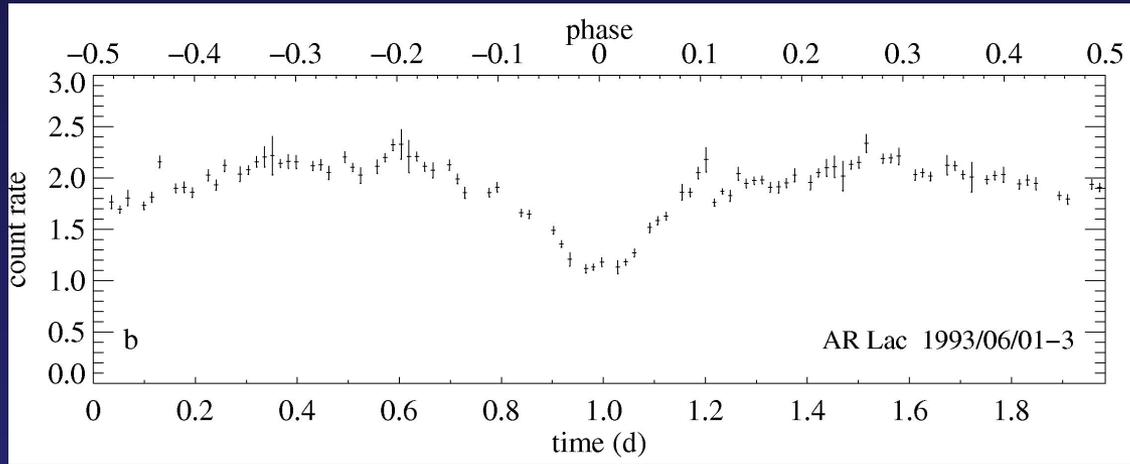




(Güdel et al. 2004)

Cargese, 6 April
2006

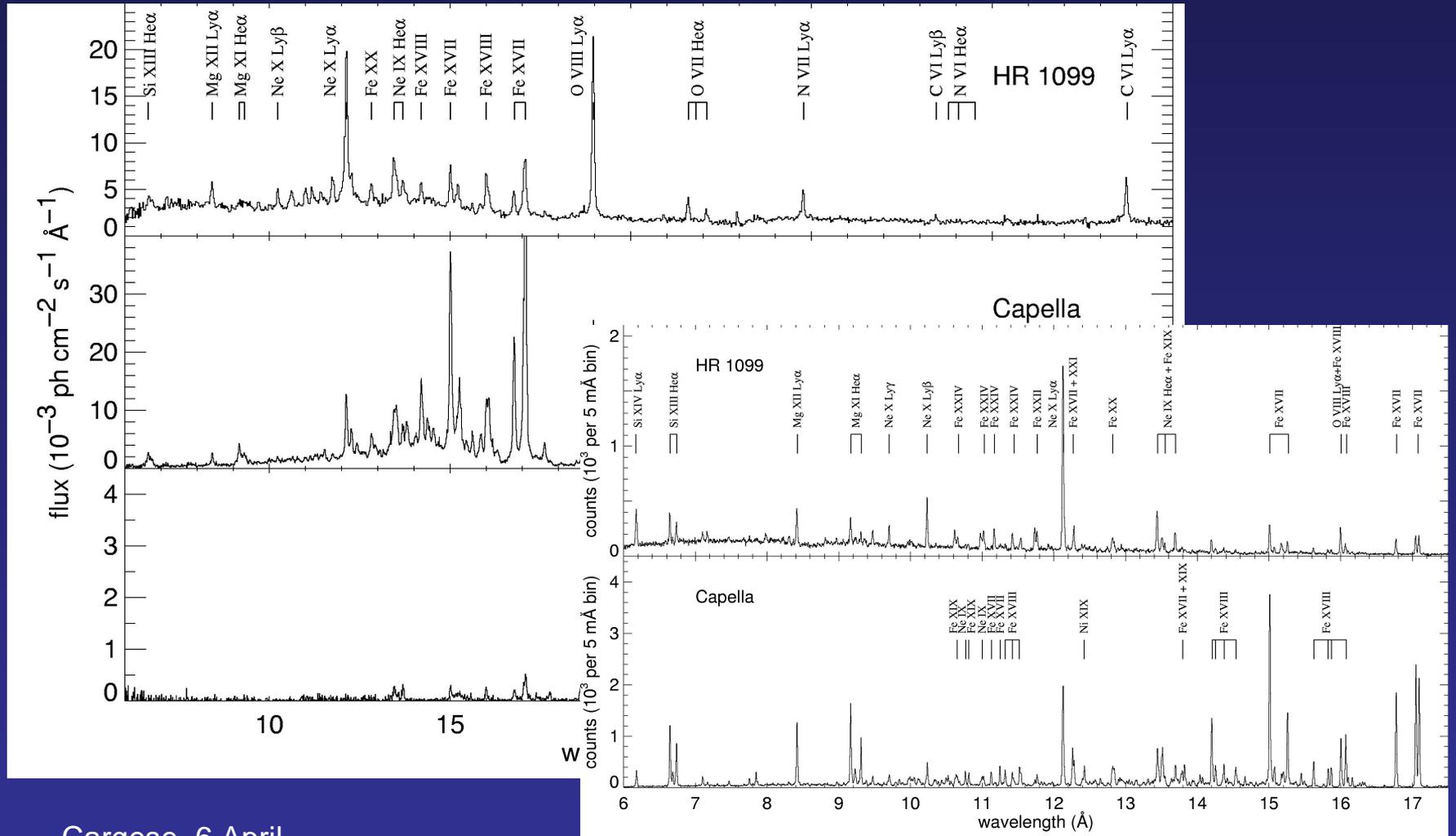
3-D modeling using Withbroe method (Siarkowski et al. 1993)



intrabinary magnetic fields?

Coronal Spectroscopy

X-rays from stellar coronae



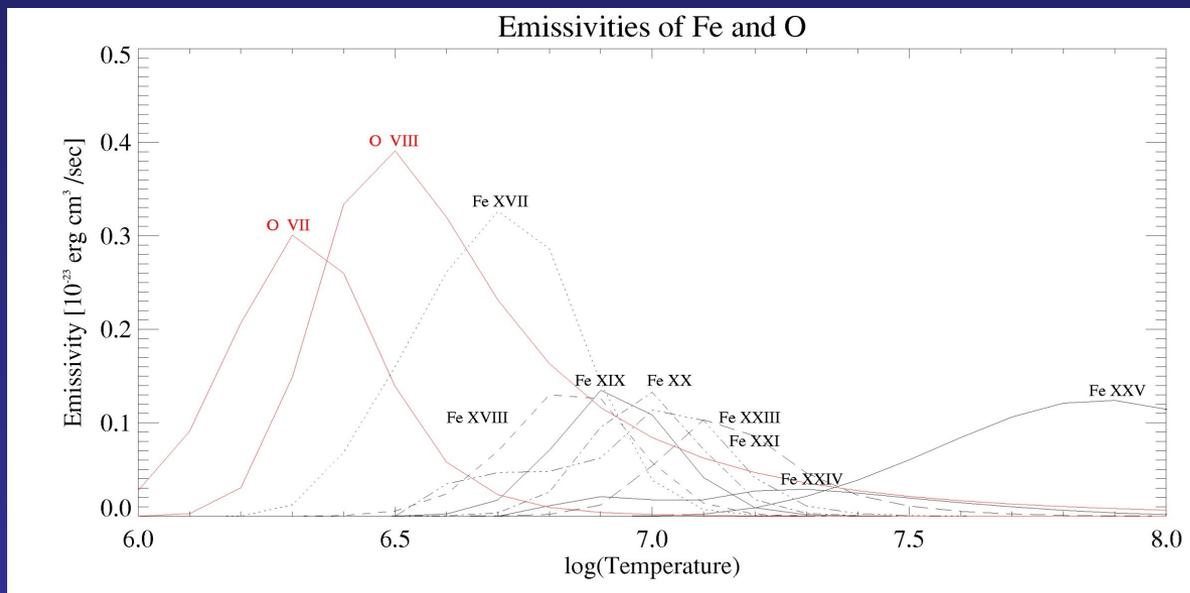
Basic definitions

Flux in a collisionally excited line:

$$\phi_j = \frac{1}{4\pi d^2} \int AG_j(T) \frac{n_e n_H dV}{d \ln T} d \ln T$$

where d = distance, A = element abundance, G = line cooling function, n_e , n_H = number densities of electrons and protons, respectively.

Each line forms typically over factor of two in T (width for a ionization stage)

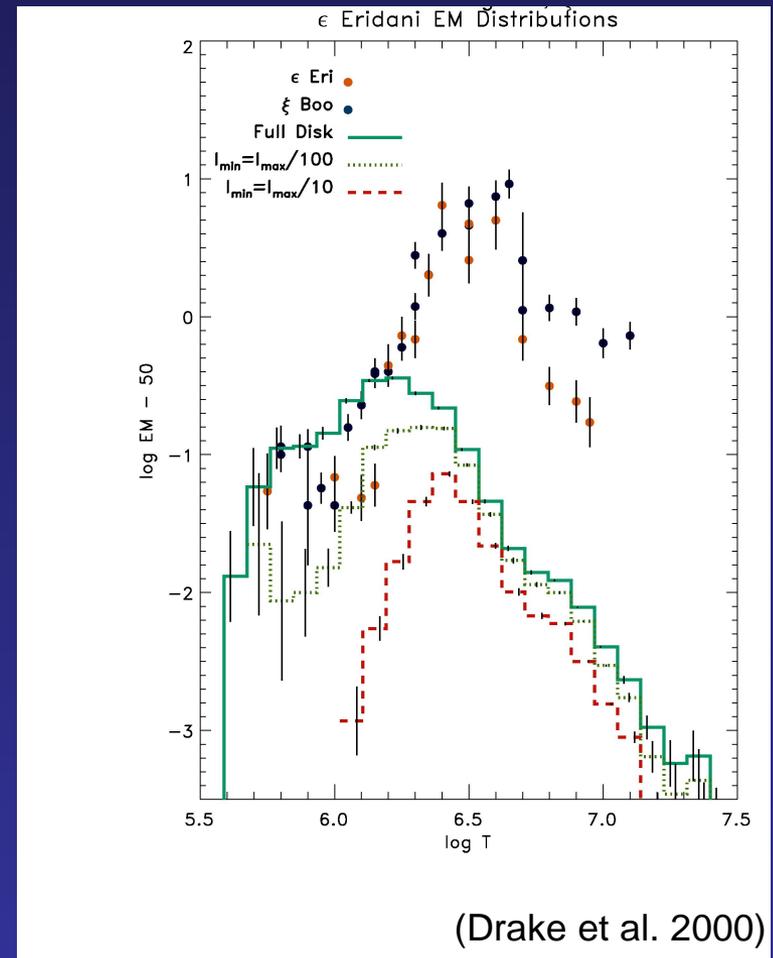


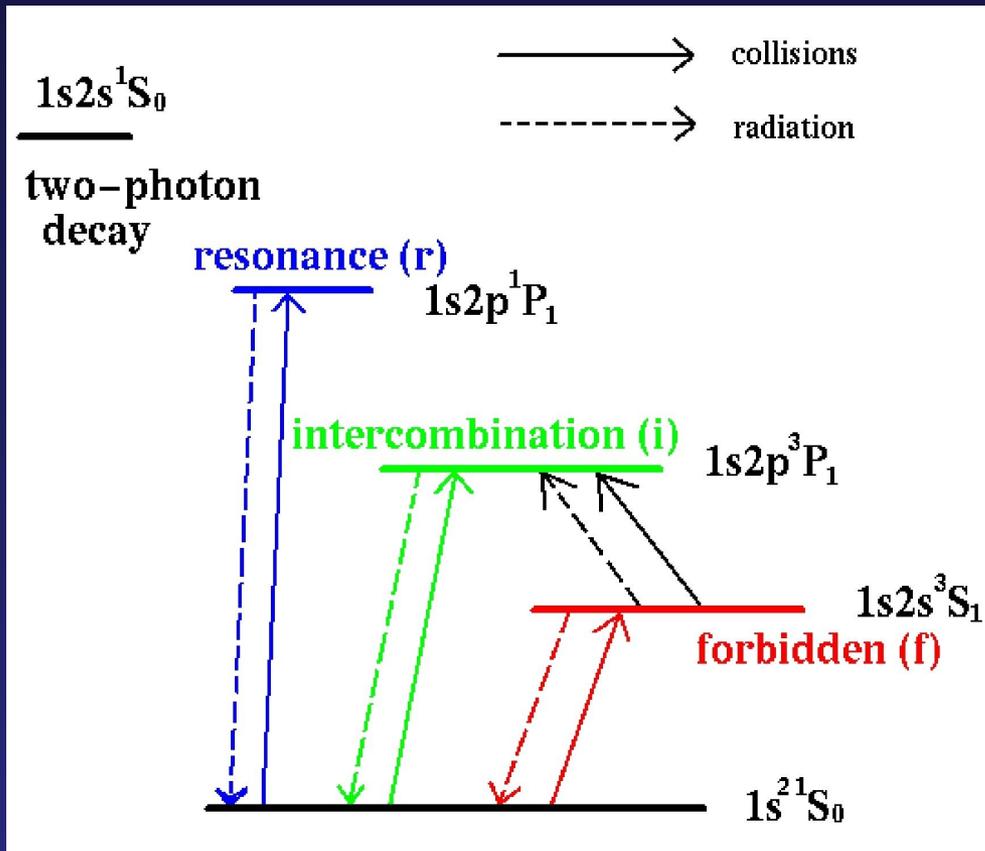
Basic definitions

Emission measure per $d\ln T$

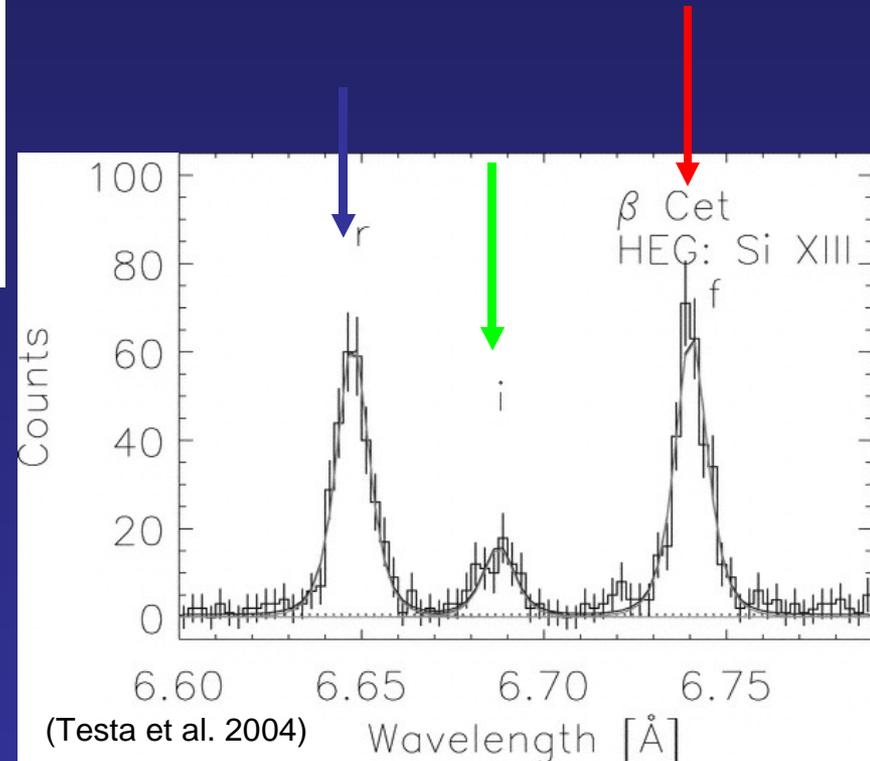
$$Q(T) = \frac{n_e n_H dV}{d\ln T}$$

Differential emission measure distribution (DEM)





Density-sensitive He-like triplets in X-rays:



$EM = n_e^2 V$ measured from spectrum

n_e measured spectroscopically

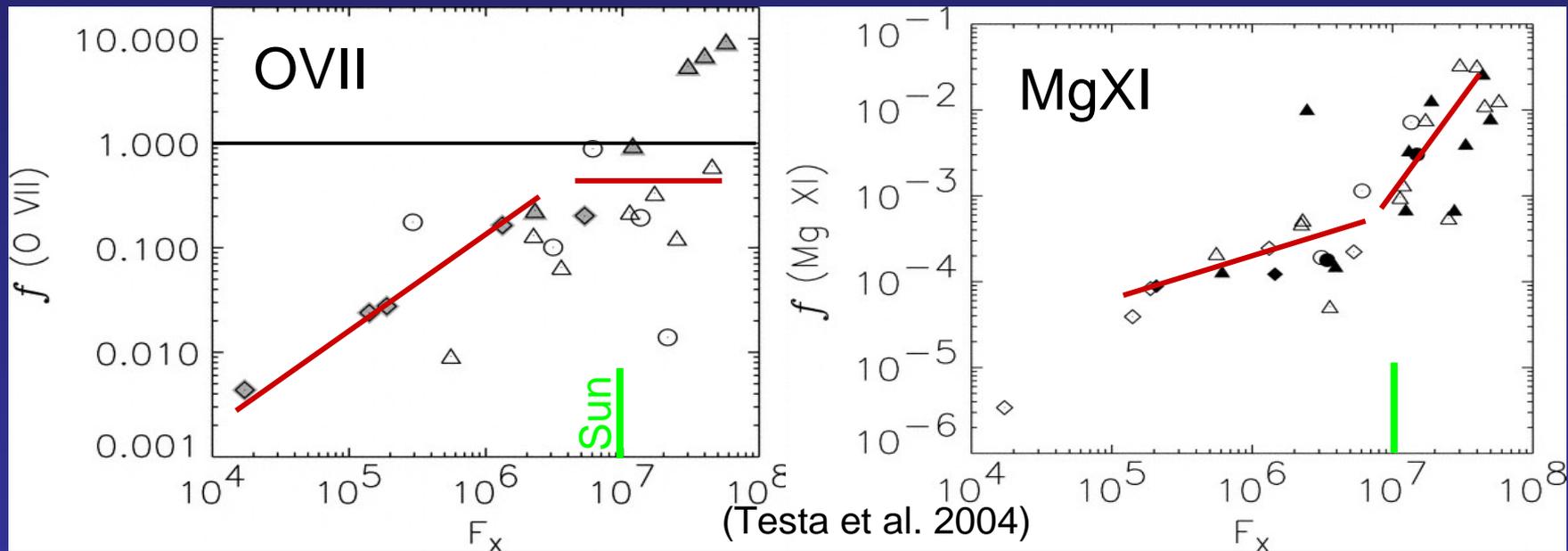
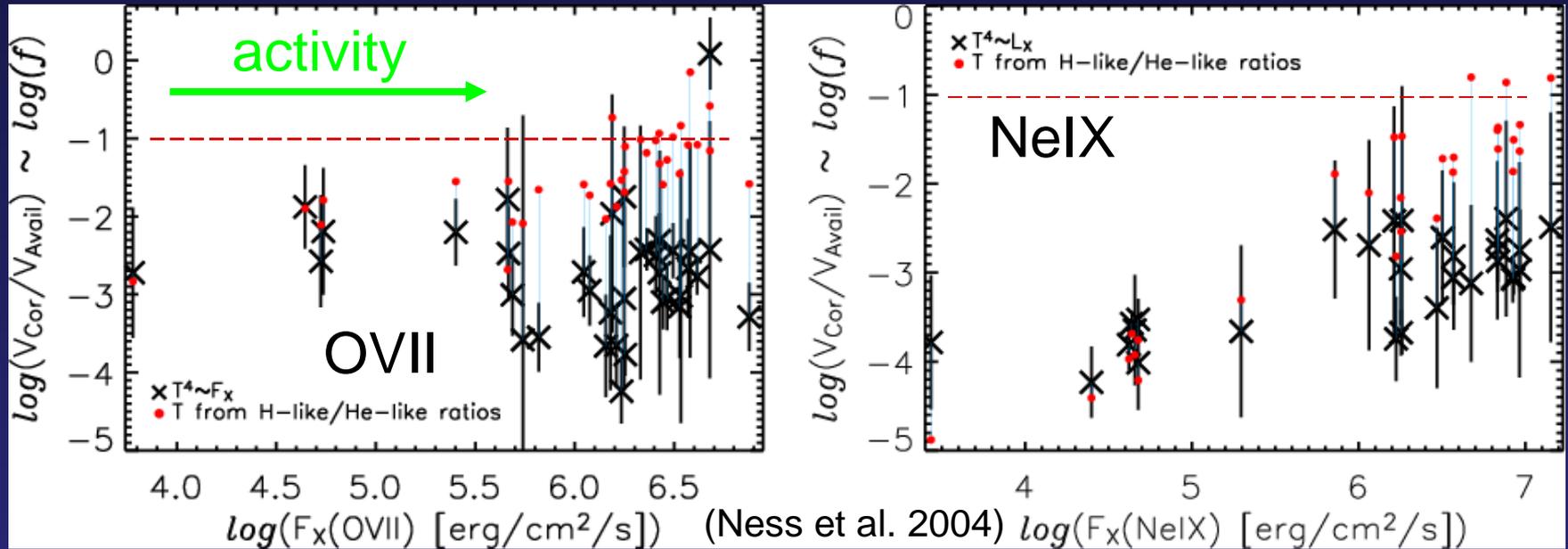
$$V = EM/n_e^2$$

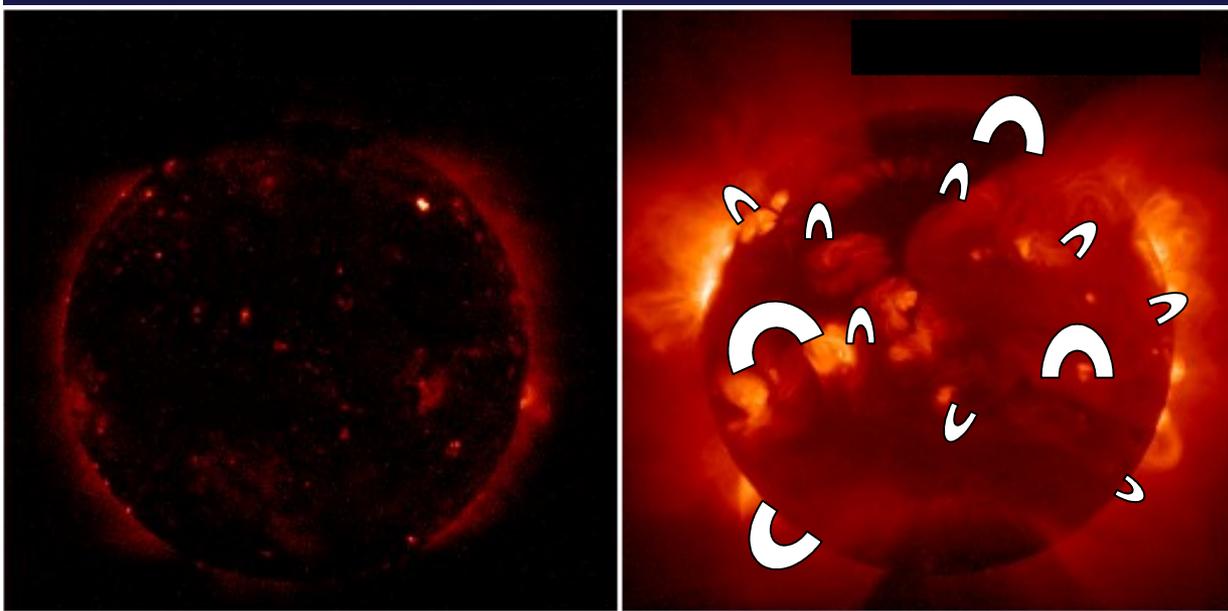
assume reasonable scale height of corona
(or coronal loop height)

→ surface filling factor of X-ray bright loops



Conclusions from density surveys: plasma filling factors





Stronger dynamo
→
Cool (2 MK) active
regions increase
filling factor (but $\ll 1$)

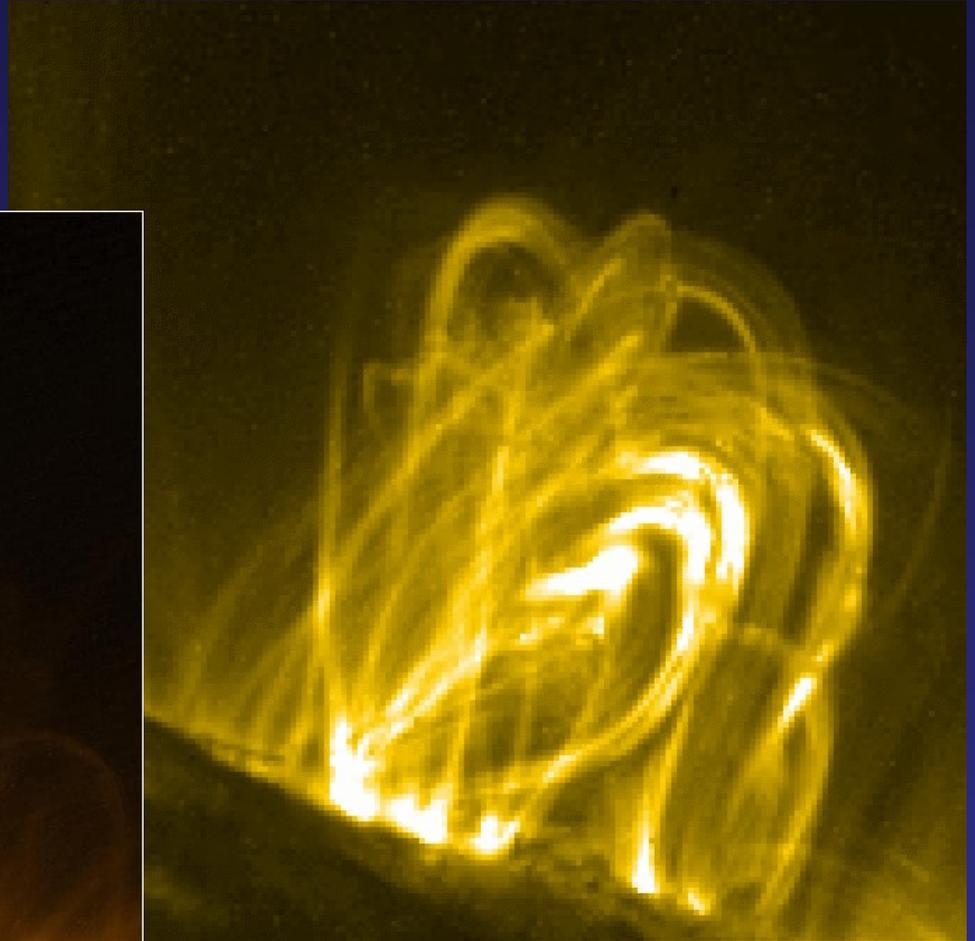
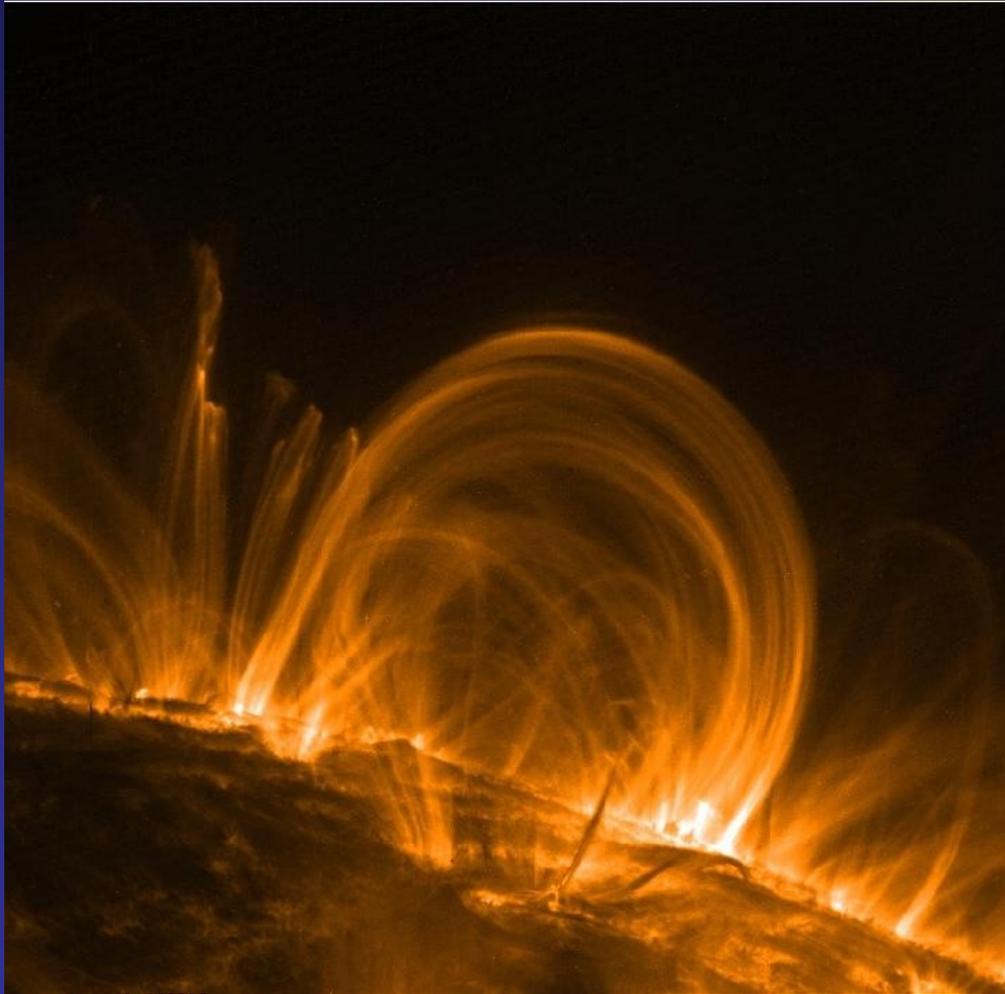
More magnetic interaction → flaring:

Emergence of growing hot, high-density (→ high-luminosity)
component between cooler regions.

(Güdel et al. 1997, Drake et al. 2000, Ness et al. 2004, Testa et al. 2004)

- *Fine Structure: Magnetic Loops*

Determining coronal structure with X-rays



Magnetic loops as building blocks

Simplifying assumptions:

energy balance

no flows

constant pressure along B

("no gravity" or "height \ll scale height")

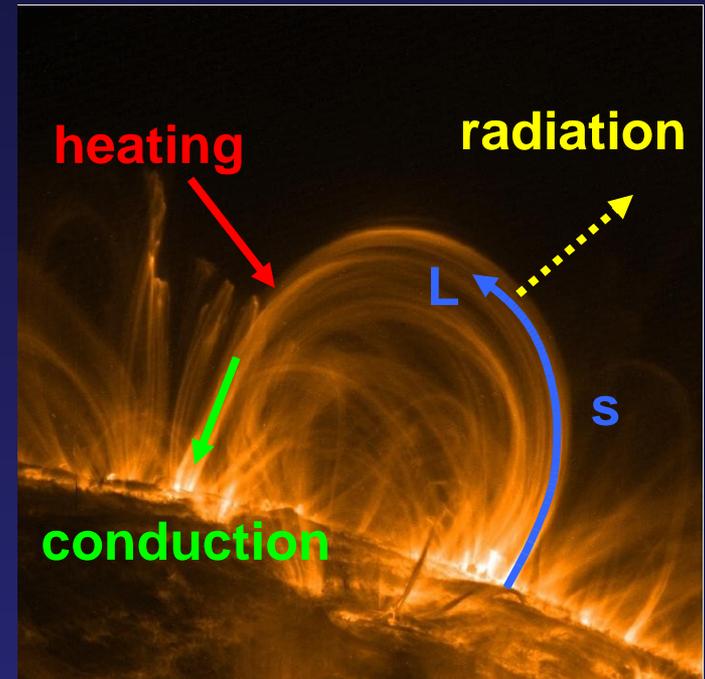
Energy balance: $E_H - E_R - \nabla F_c = 0$

$F_c(s) = -\kappa T^{5/2} dT/ds$ conductive heat flux

$E_R = n^2 \Lambda(T)$ emissivity

$E_H = ???$ heating term

Here, E_H being unknown, one usually assumes **uniform heating**, or some geometric distribution (footpoint heating, apex heating, etc)

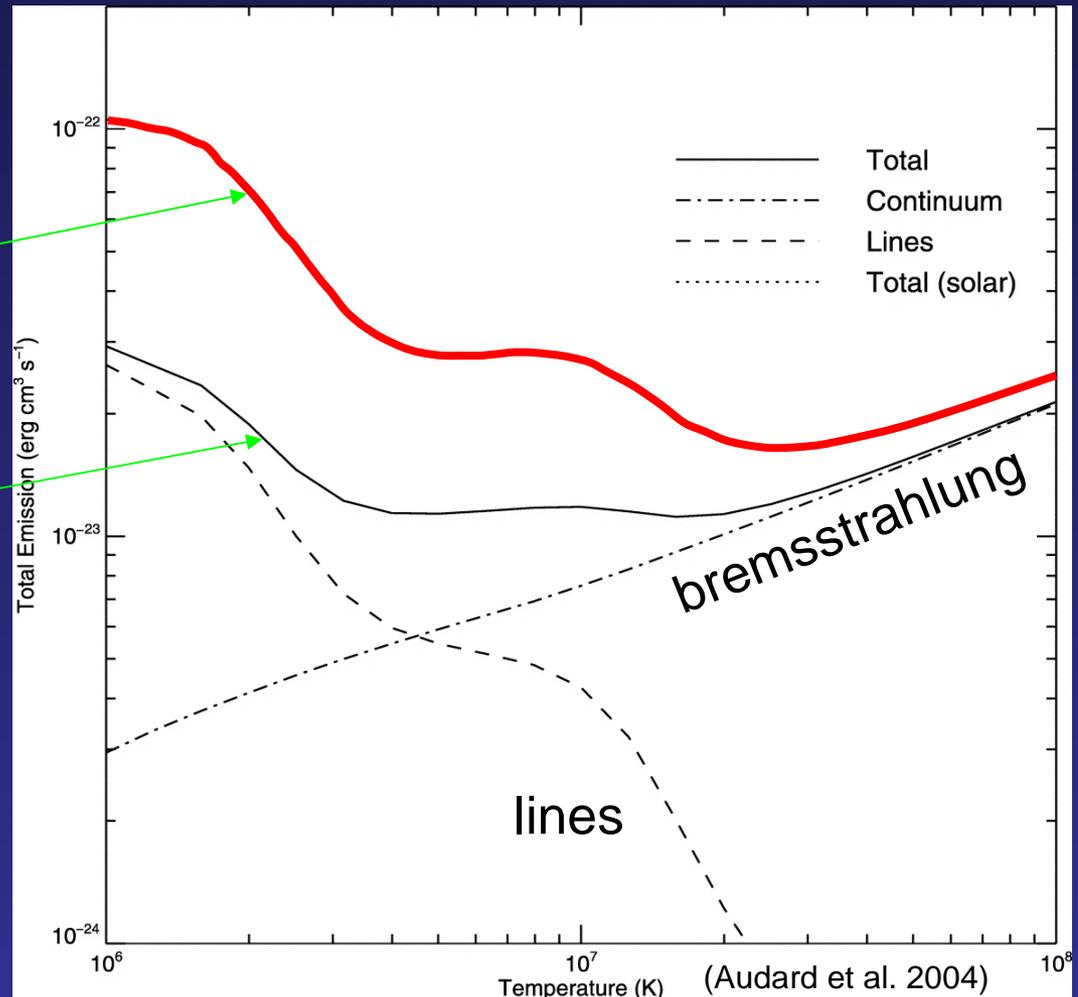


X-ray cooling function:

Radiative power for unit EM

solar abundances

active-stellar abundances



System of coupled nonlinear differential equations

$$dT/ds = - F_c / kT^{5/2}$$

heat conduction law

$$dF_c/ds = E_H - n^2\Lambda(T)$$

heat balance



conduction heating radiation

$F_c = 0$ at apex

solve for $T(s)$ and $n(s)$ (Rosner et al. 1978, Vesecky et al. 1979, van den Oord et al. 1997)

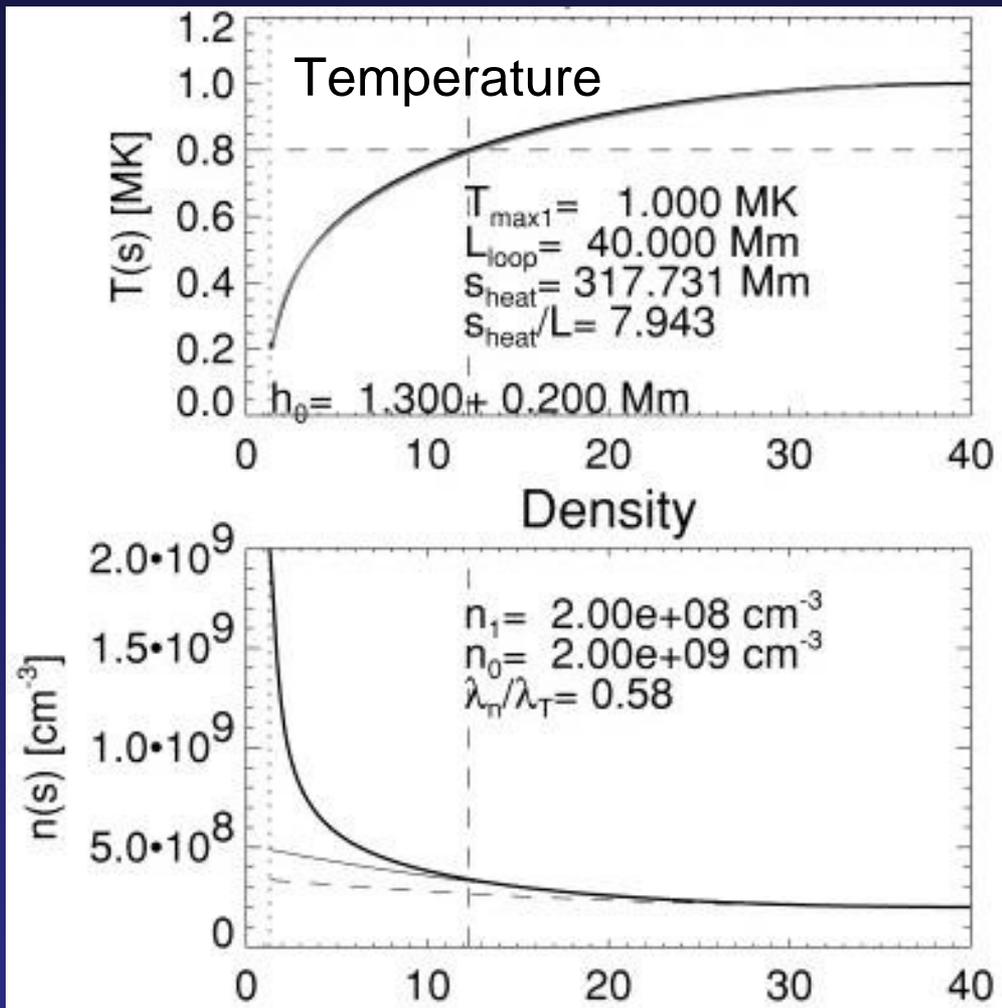
$$\begin{aligned} \text{DEM}(T) &\propto pT^{3/2} \\ &\propto pT \end{aligned}$$

if significant conductive flux through footpoint
if *no* conductive flux through footpoint

$$T_{\text{apex}} = 1400 (pL)^{1/3}$$

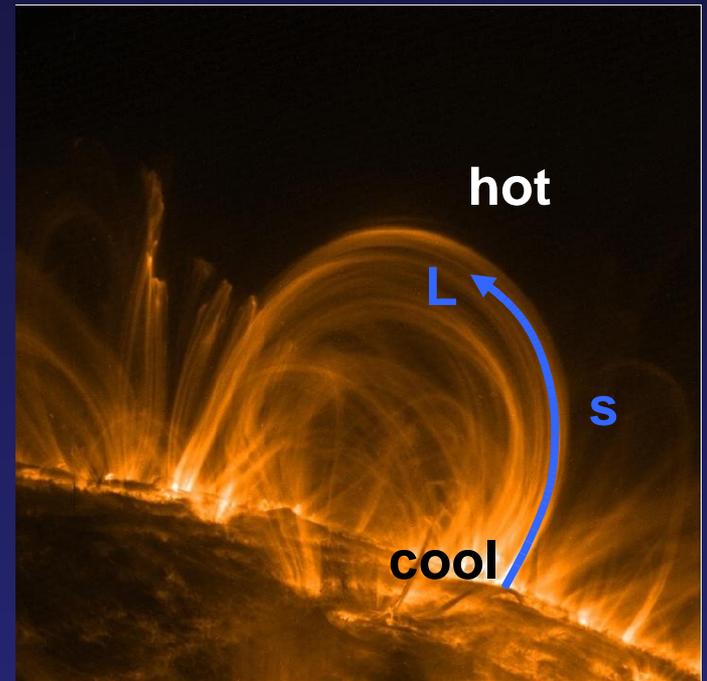
$$E_H = 98000 p^{7/6} L^{-5/6}$$

"Scaling laws" for "RTV loops"



footpoint

loop top

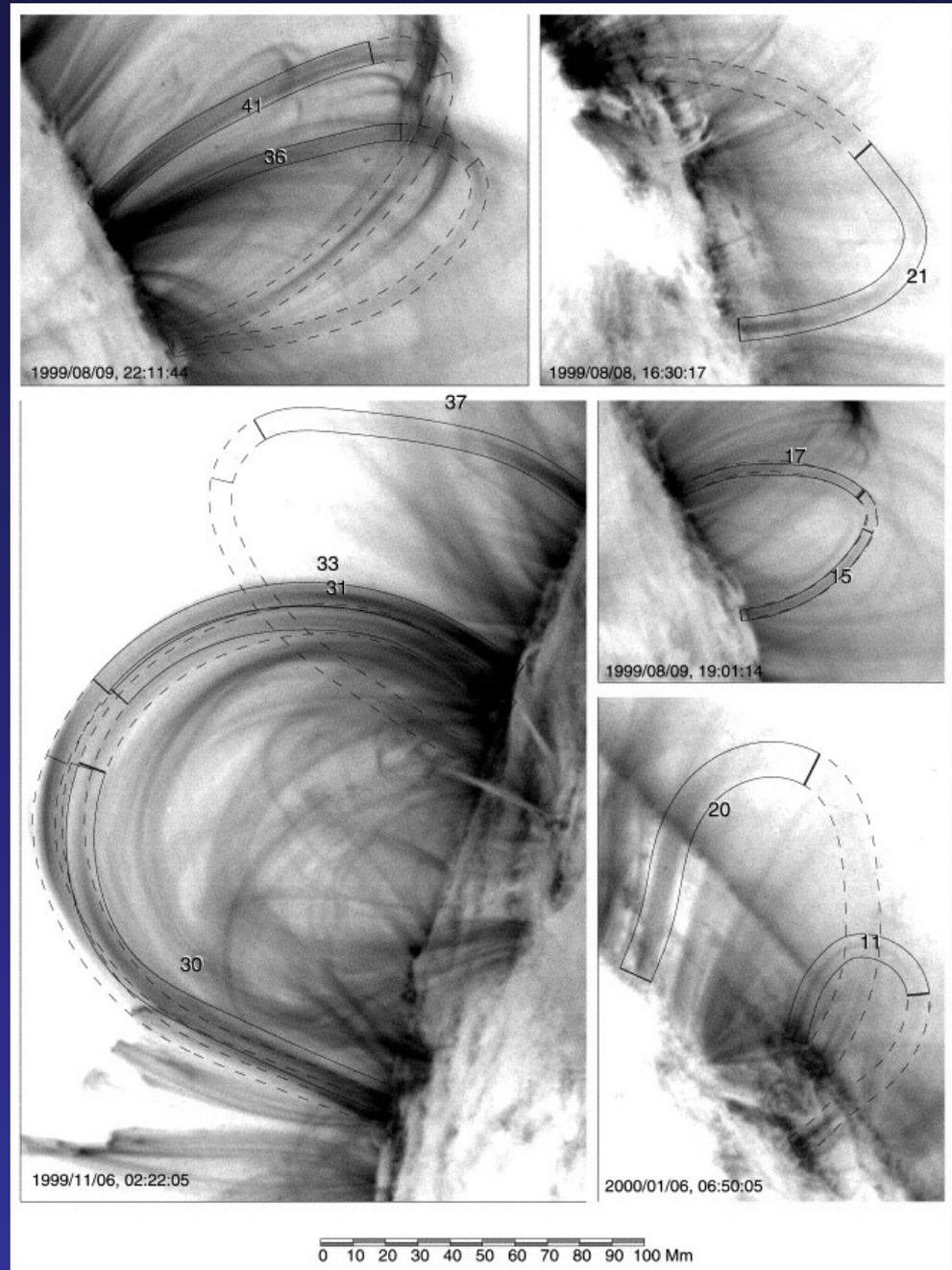


Verification for the solar corona:

(Aschwanden et al. 2000, 2001)

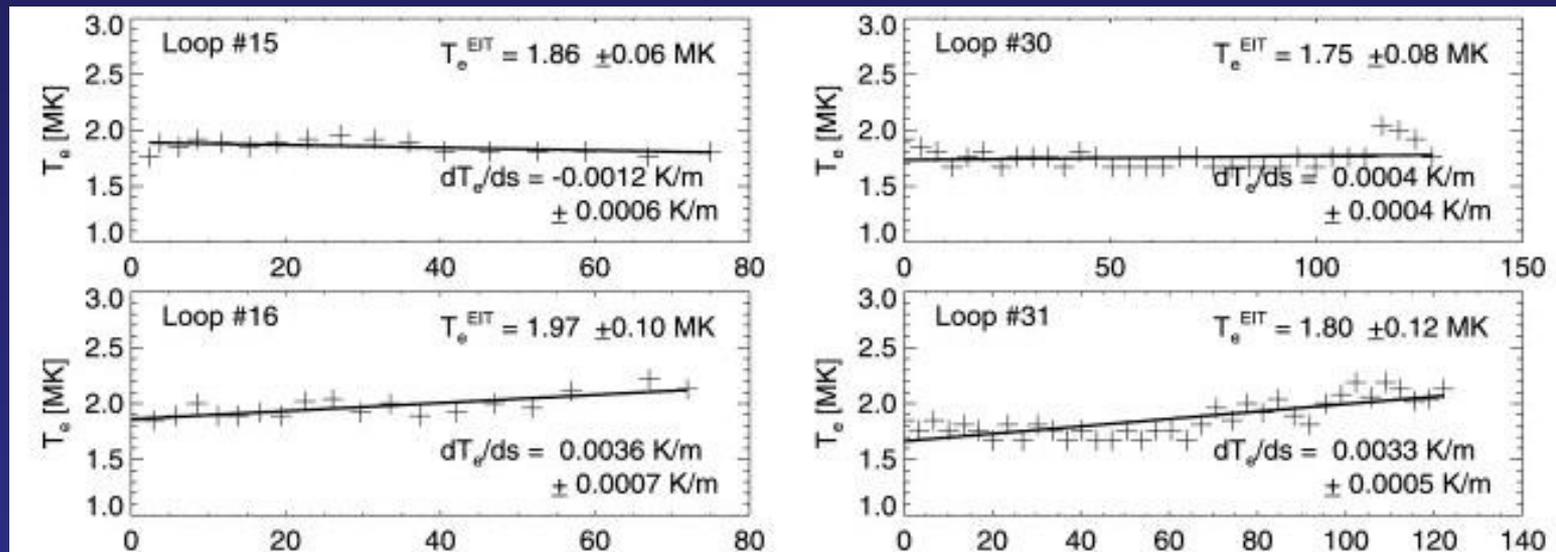
- * determine $T(s)$, $n(s)$ from TRACE data (flux, filter ratios)
- * reconstruct $p(s)$, DEM(T)
- * compare with theory

Tests predominantly cool loops ($T < 2$ MK).



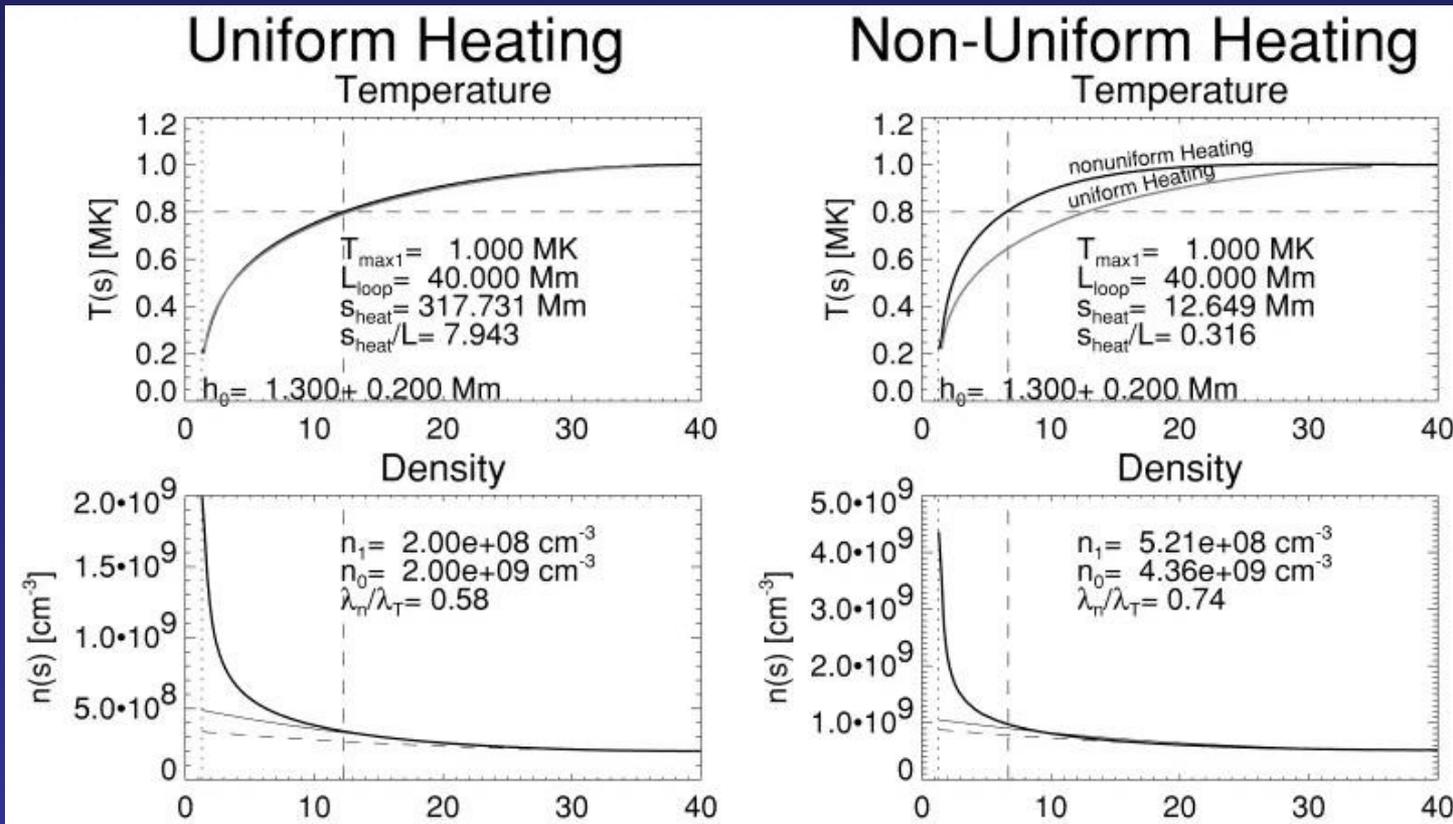
Verification for the solar corona (Aschwanden et al. 2000, 2001):

- Solar coronal loops **nearly isothermal**: RTV uniform heating **not** applicable



Verification for the solar corona (Aschwanden et al. 2000, 2001):

- **Non-uniform heating** near loop footpoints yields **flatter** T profile
- Flatter T profile provides **steeper DEM**
- Heating scale height above footpoint: $(1.7 \pm 0.6) \times 10^9 \text{ cm} = 0.024 R_{\odot}$



Verification for the solar corona: (Aschwanden et al. 2000, 2001)

In 60%, density *too high* for whatever static loop model (uniform or non-uniform heating)

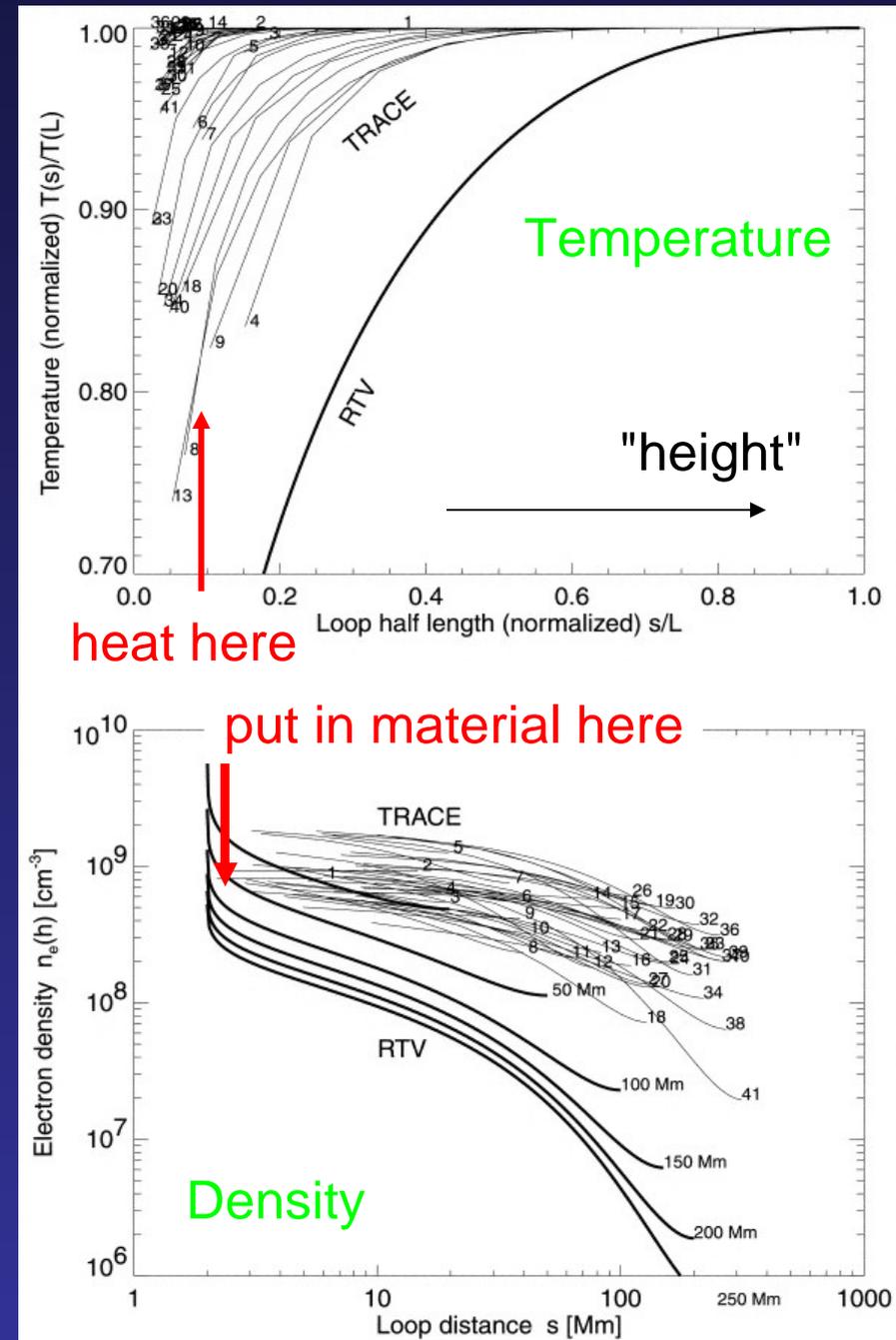
Flat T and high pressure:
Conduction unimportant

Energy balance:

$$E_H + E_R = 0$$

Energy and mass flow through footpoints into loops?

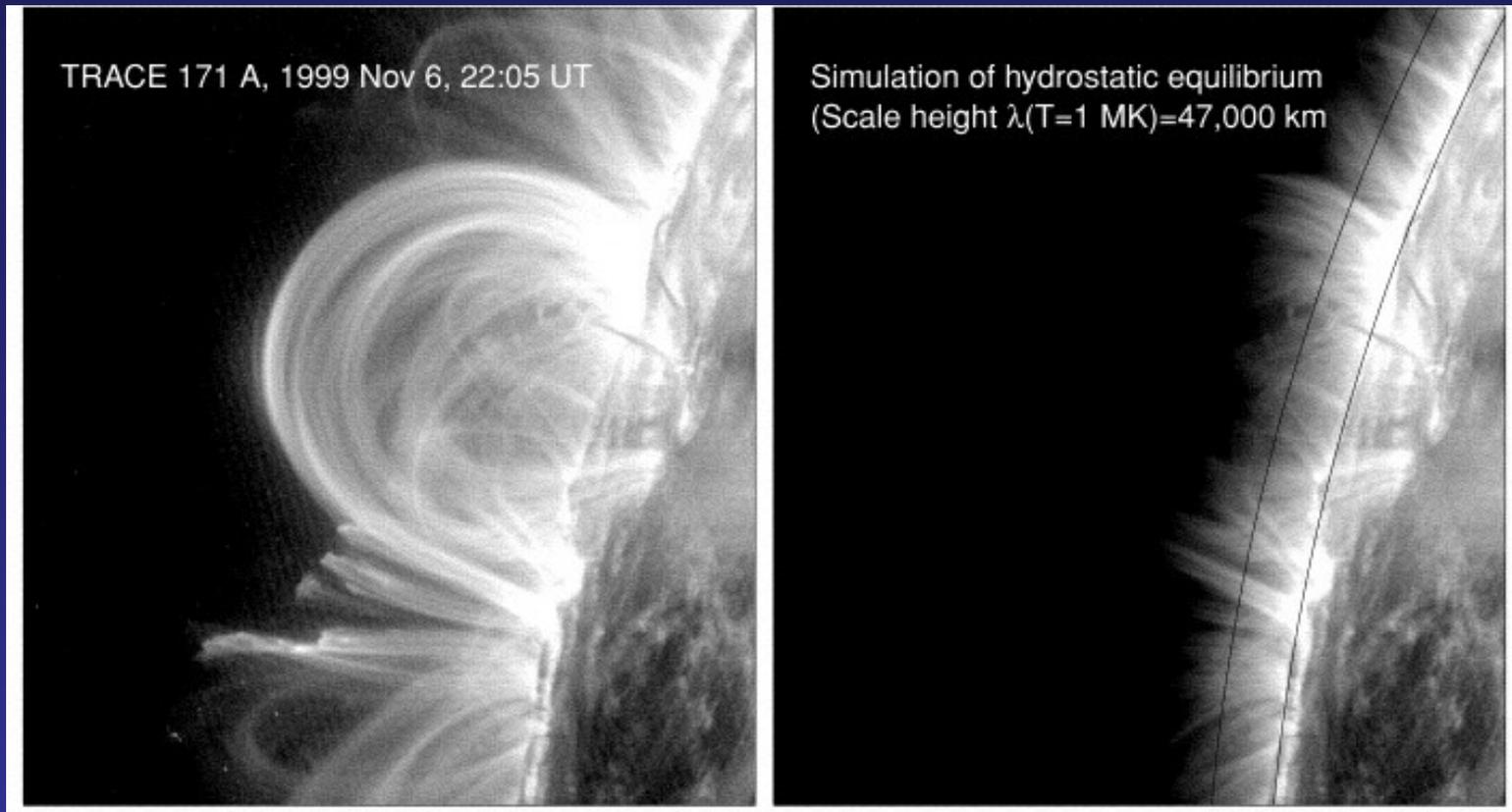
Dynamic loops; stochastic energy release?



Verification for the solar corona:

(Aschwanden et al. 2000, 2001)

Many large loops show scale heights that are much larger than predicted by theoretical static models: *Mass inflow at footpoints?*

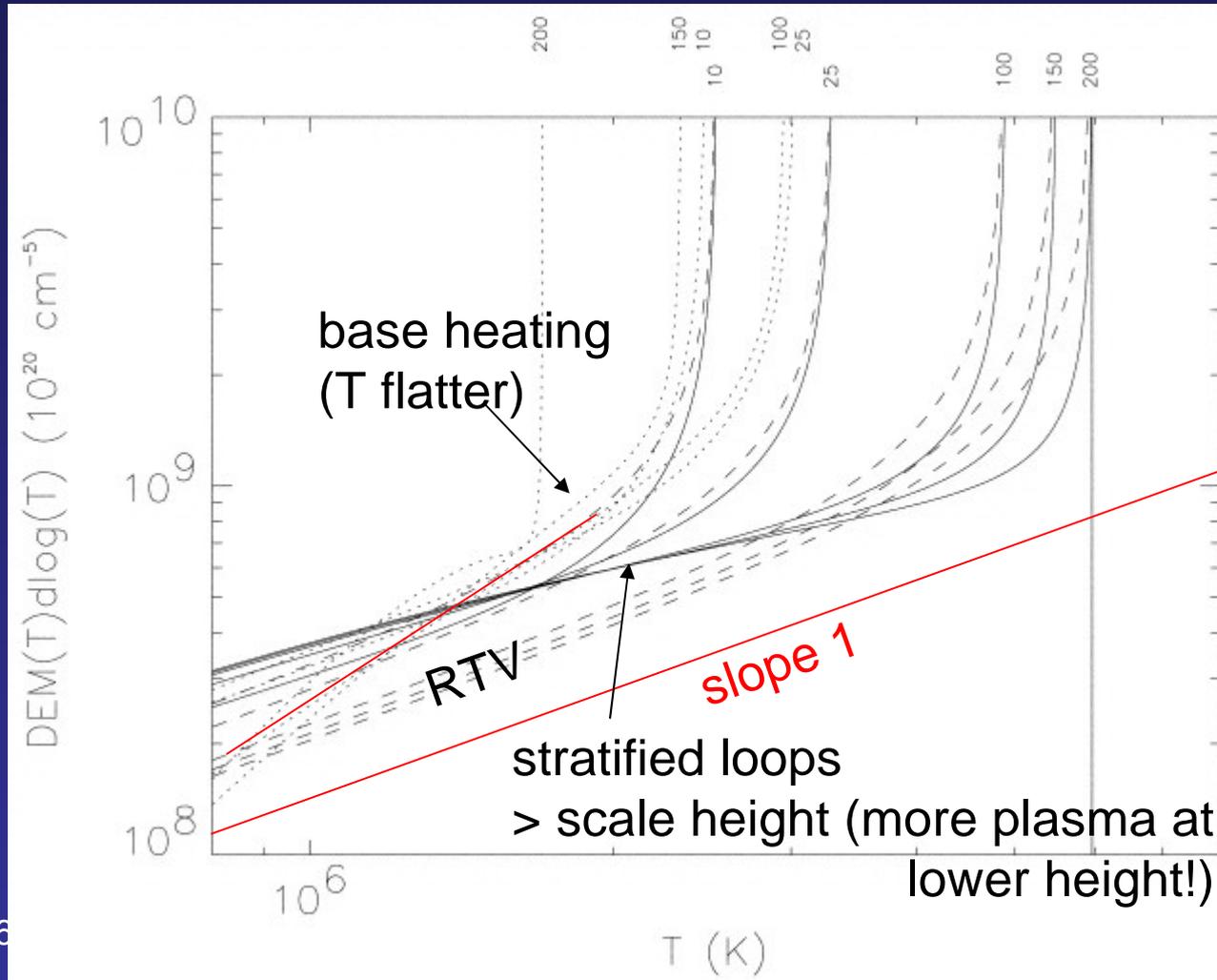


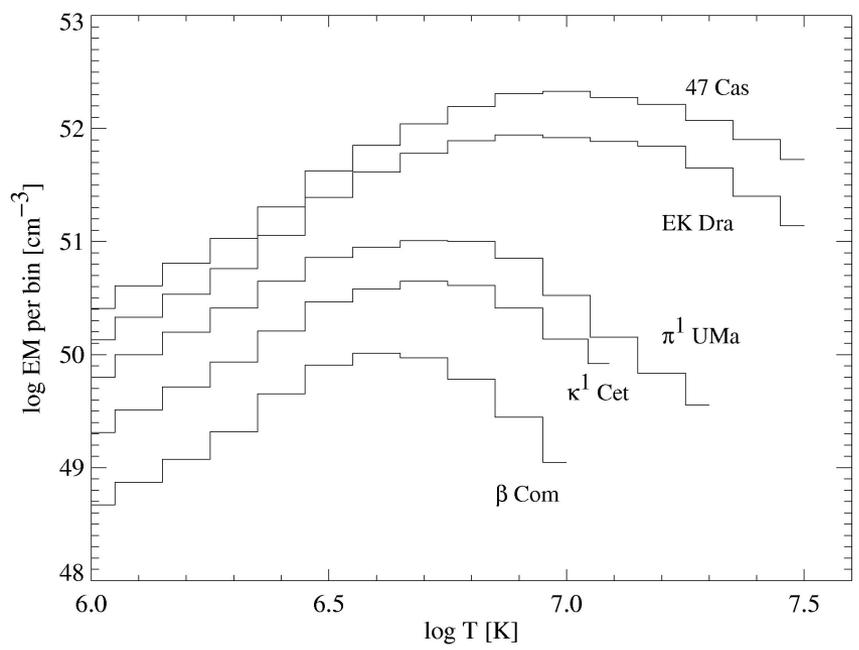
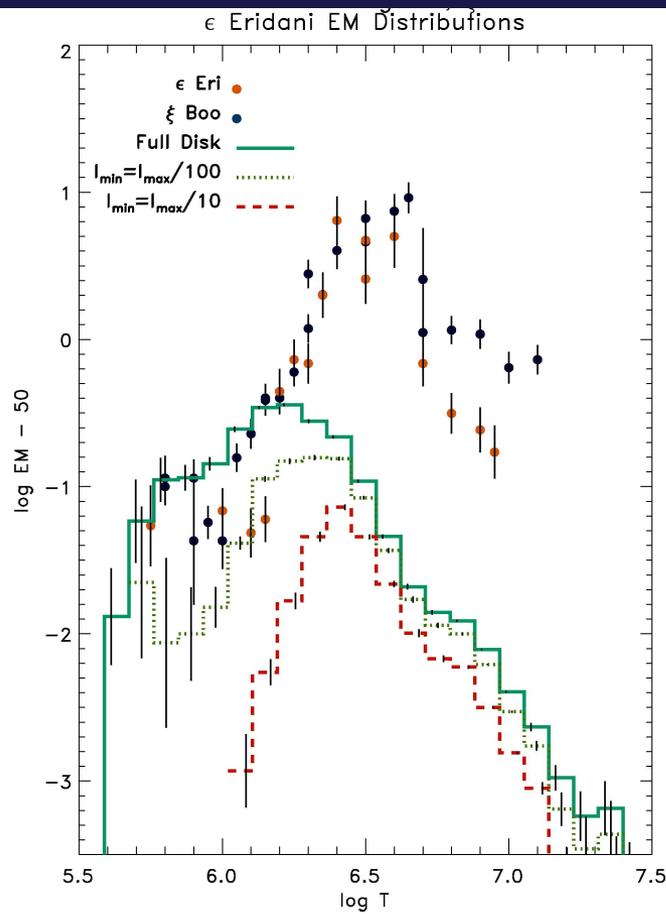
Cargese, 6 April
2006

observed

simulated for static conditions

DEMs of loops for uniform (RTV) and non-uniform heating , small (RTV) and large stratified loops (Schrijver & Aschwanden 2002)





(Telleschi et al. 2005)

Power-laws on each side of peak
 Very steep on cool side

More active (luminous)
 → higher peak (average) temperature

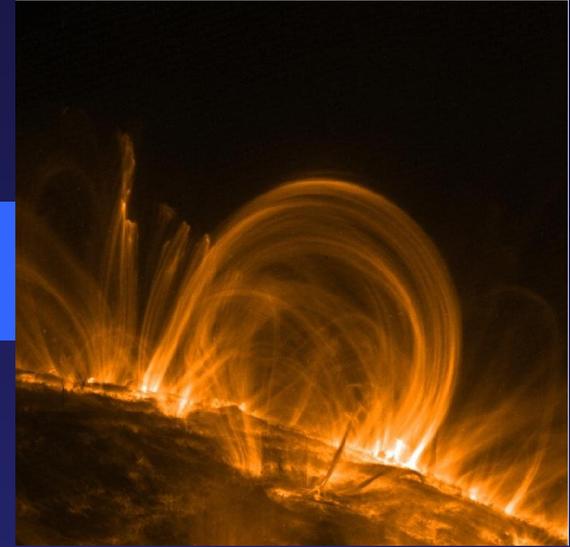
(Drake et al. 2000)

Conclusions for the stellar astronomer:

- **Static loop** models to be used with **caution**
- In magnetically **active stars**, risk that static approach is inappropriate is even larger
- Need to consider **dynamic** heating models: stochastic (quasi-continuous) reconnection between adjacent fields? Microflaring?

More on this from the perspective of stellar coronal astronomy later

Coronal Flares

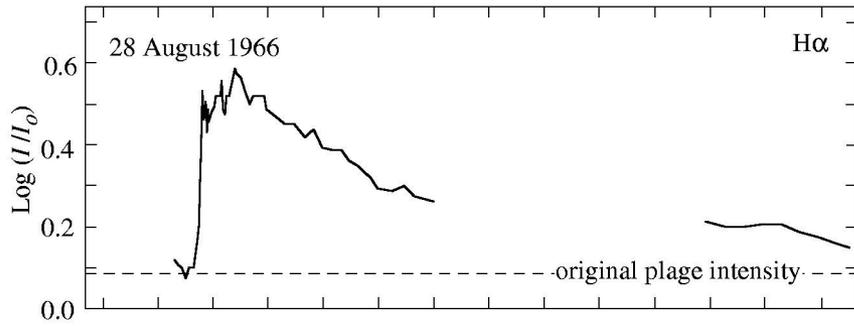


Explosive release of energy in a solar/stellar magnetic atmosphere,

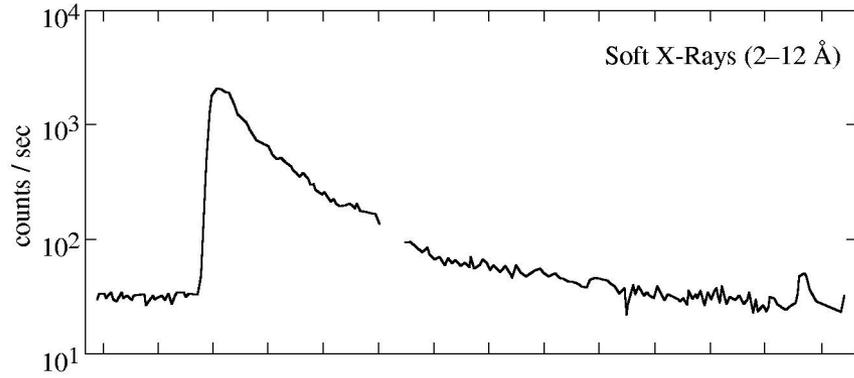
- seen at many **wavelengths** (radio, optical, UV, X-rays, gamma rays)
- affecting **many layers** of the atmosphere (photosph., chromosph., corona)
 - accelerating and ejecting **particles** and **mass** packets into space

10^{32} erg on Sun, up to 10^{36} erg on stars
lasting from **minutes to hours**

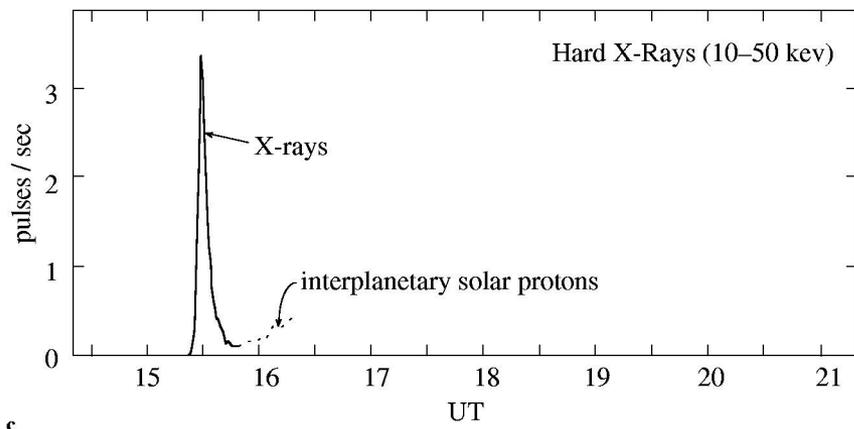
In X-rays, flares occur in closed magnetic systems that contain heated plasma.



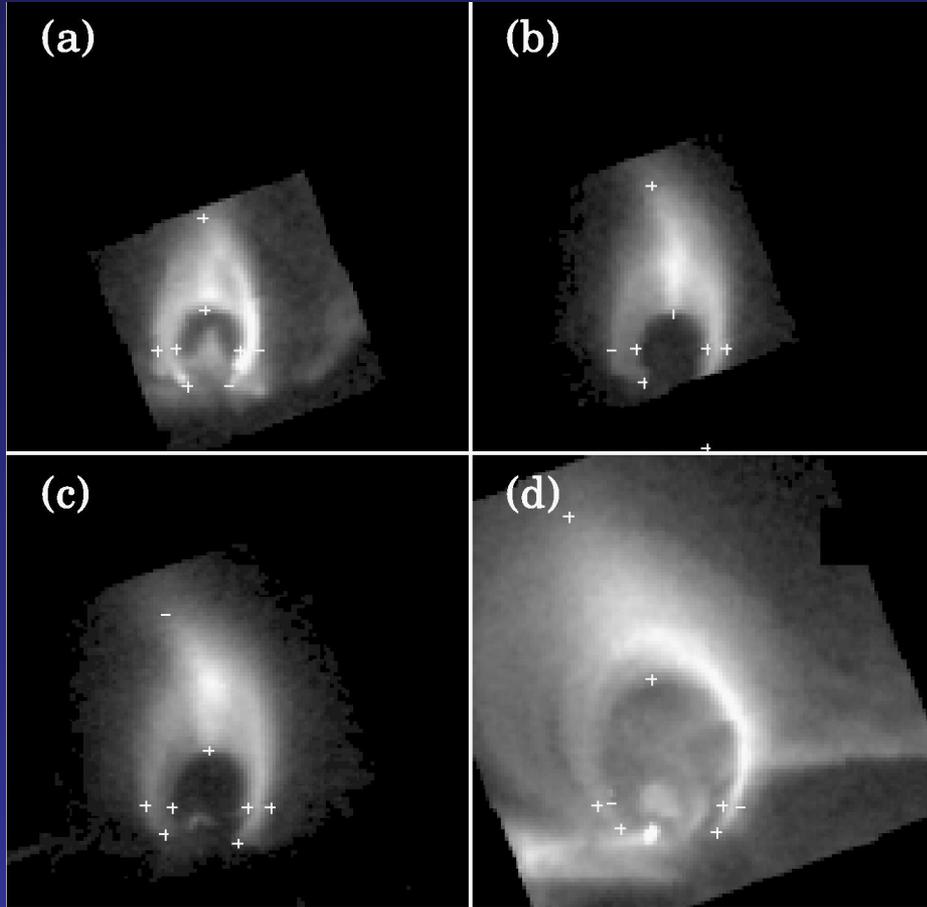
a



b



c



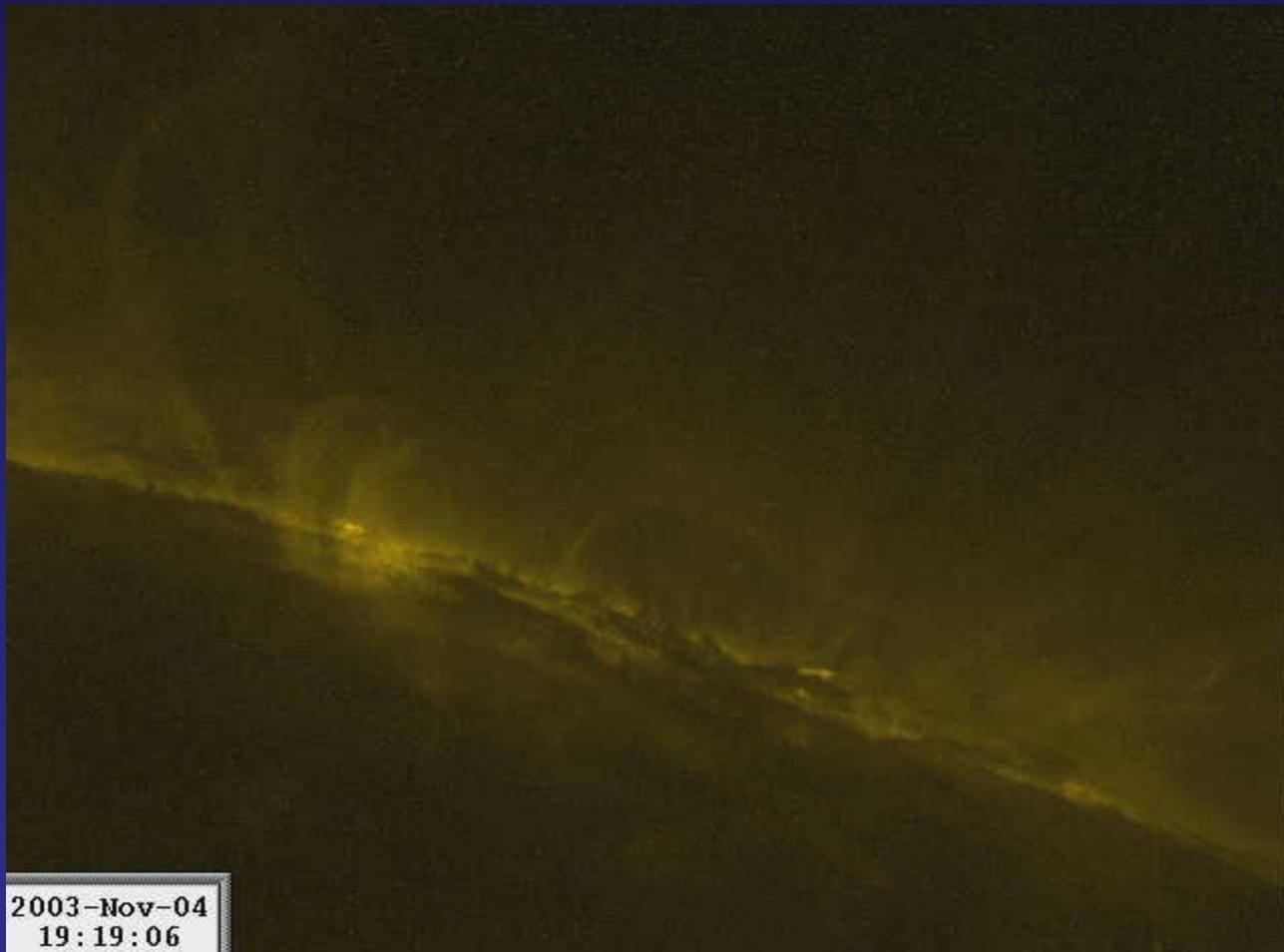
Cargese, 6 April 2006

(Priest & Forbes 2000)

(Forbes & Acton 1996)



Cargese, 6 April
2006



Cargese, 6 April
2006

Two major questions:

Why do flares occur?

Triggered release of stored energy

How do flares operate?

Heating of plasma, acceleration of particles

Magnetic Fields as Carriers of Energy: Reconnection

Maxwell's equations:

$$\left\{ \begin{array}{l} \nabla \times B = \frac{4\pi}{c} j \\ \nabla \times E = -\frac{1}{c} \frac{\partial B}{\partial t} \end{array} \right.$$

Ohm's law:

$$j = \sigma \left(E + \frac{1}{c} v \times B \right)$$

solve for B:

$$\frac{\partial B}{\partial t} = -c \nabla \times E$$

$$E = \frac{j}{\sigma} - \frac{1}{c} v \times B$$

$$j = \frac{c}{4\pi} \nabla \times B$$

$$\nabla \times (\nabla \times B) = \nabla(\nabla \cdot B) - \nabla^2 B$$

(see presentation by M. Tagger)

Magnetic Fields as Carriers of Energy: Reconnection

$$\frac{\partial B}{\partial t} = \nabla \times (v \times B) + \frac{c^2}{4\pi\sigma} \nabla^2 B$$

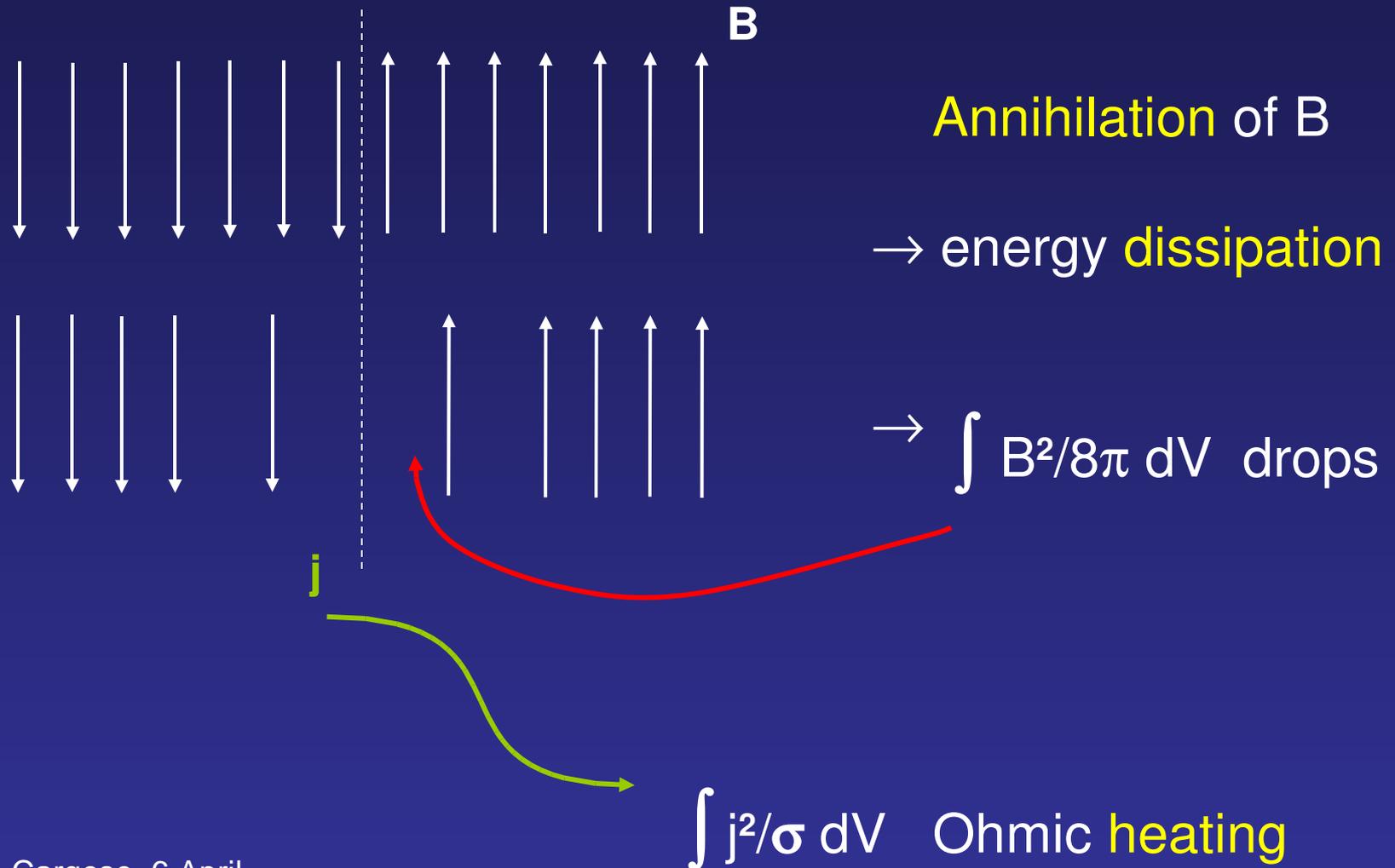
Induction
equation

(1) **Flow of matter** (B frozen in plasma) (2) **Diffusion** (finite σ)

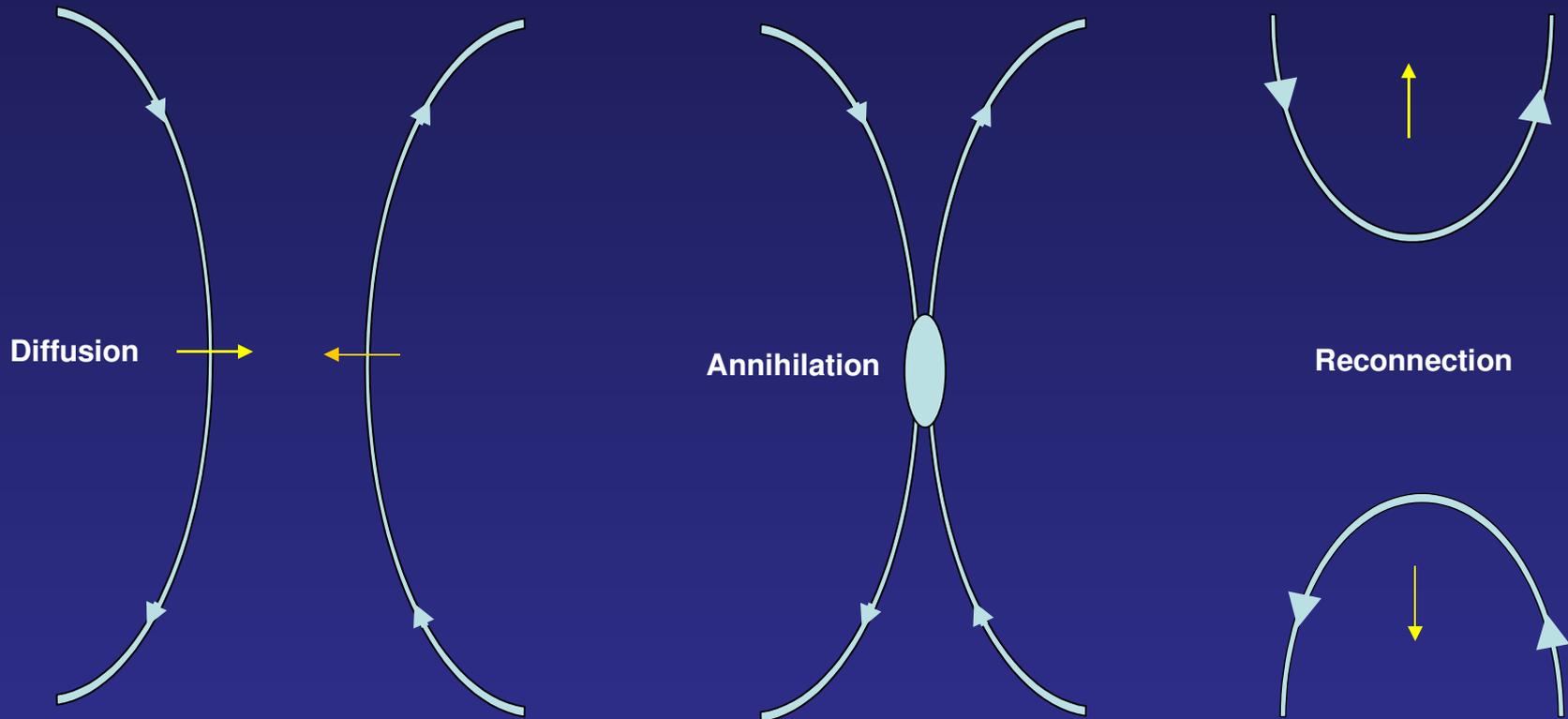
Ratio (1)/(2): mag. Reynolds number (on large scales: 10^8 in solar flares)

*Diffusion is mostly negligible across the Universe.
Exception: On short length scales!*

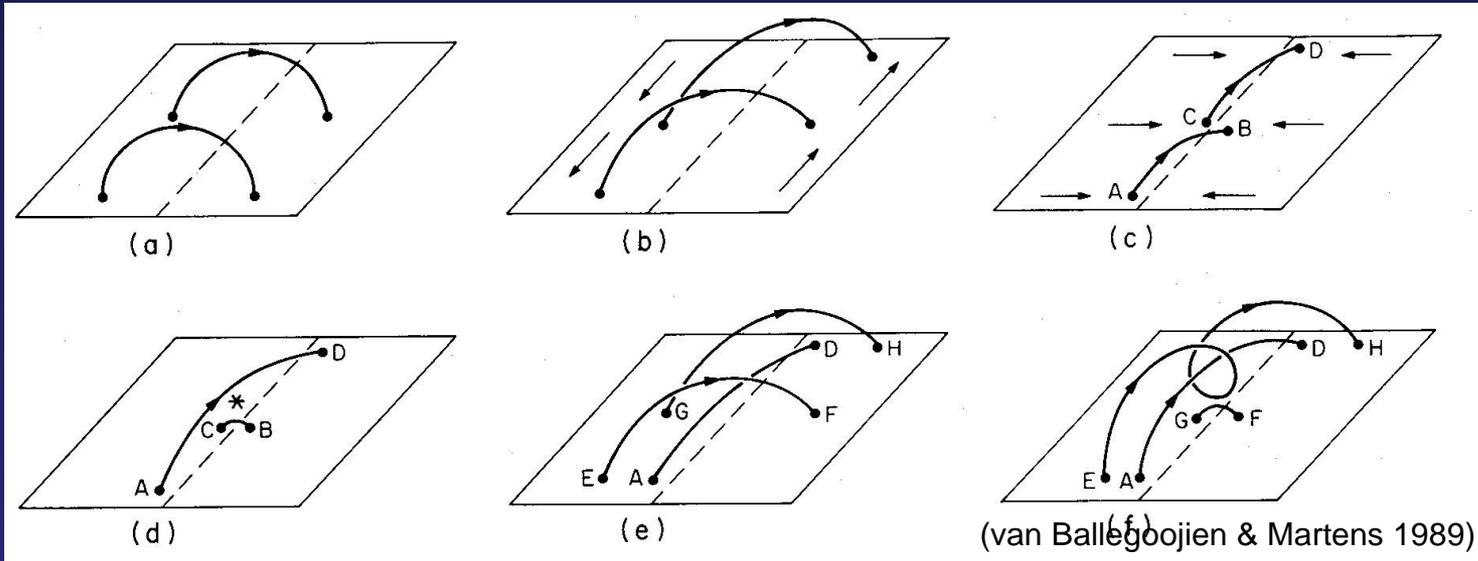
Magnetic reconnection



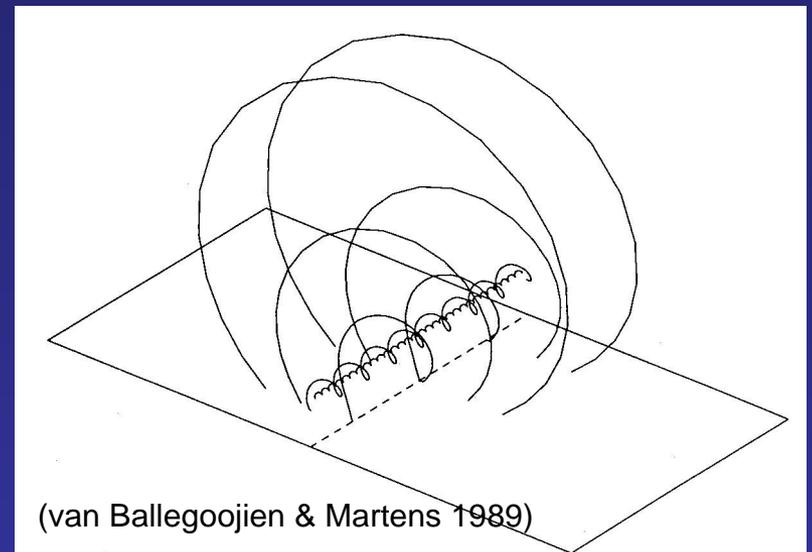
Reconnection of Magnetic Fields

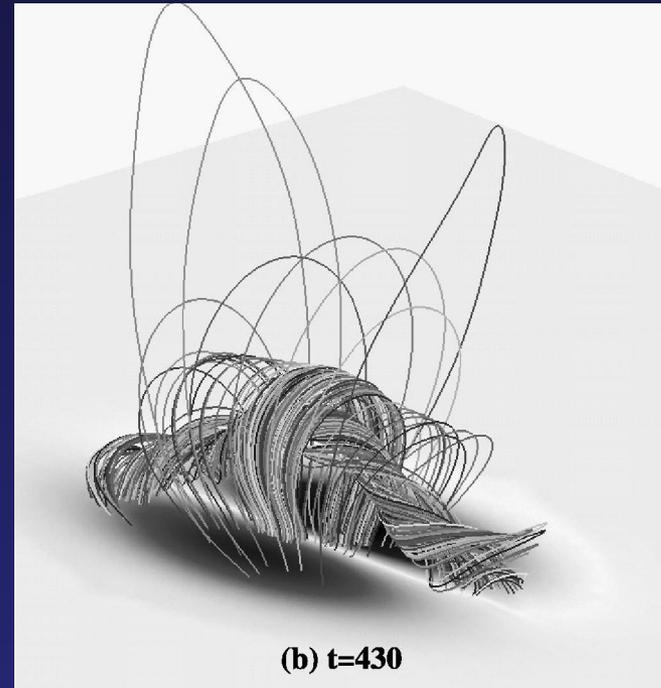
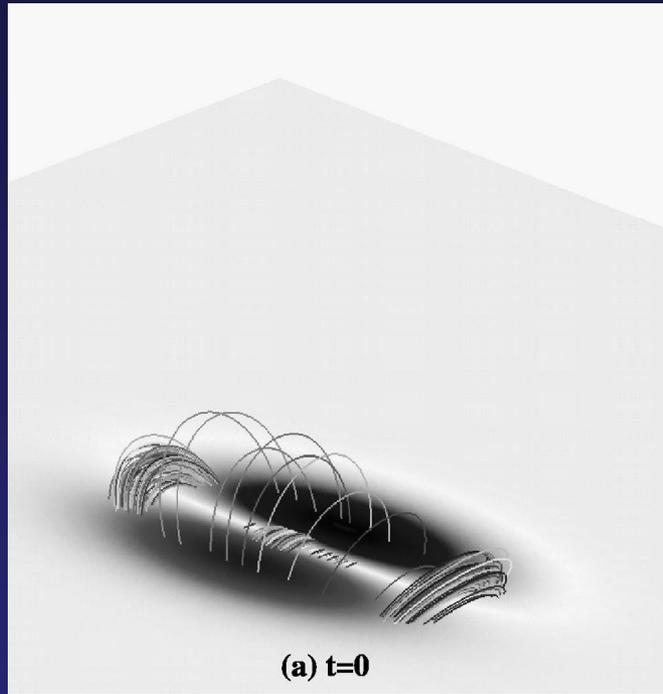


Active photosphere is in motion. Assume shear motion between two regions of opposite polarities:



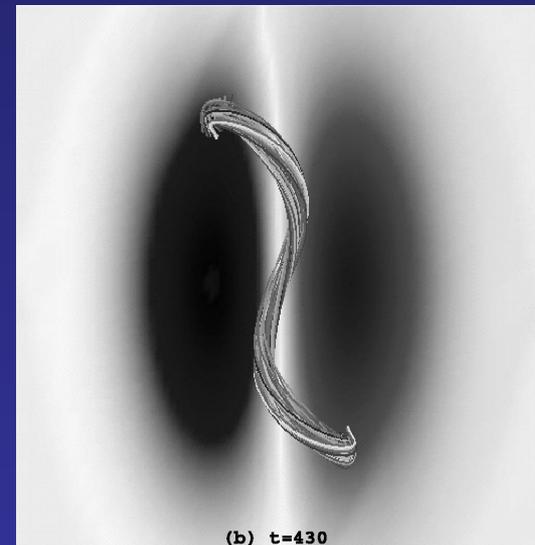
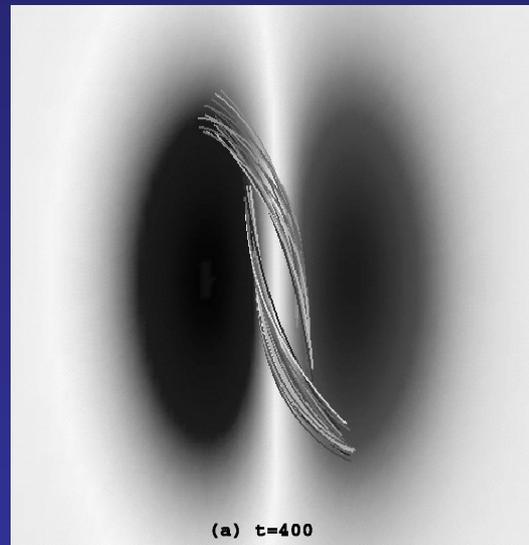
Sheared arcade reconnects to form twisted flux rope within an overlying arcade

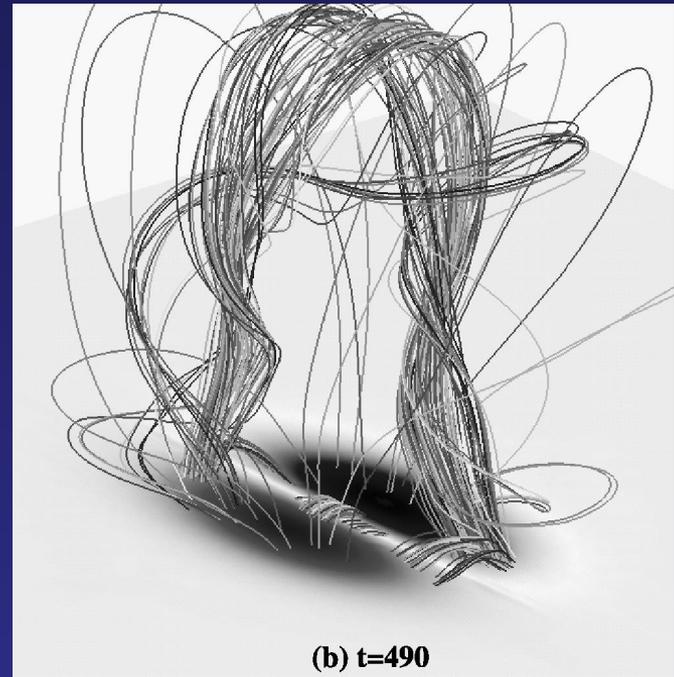
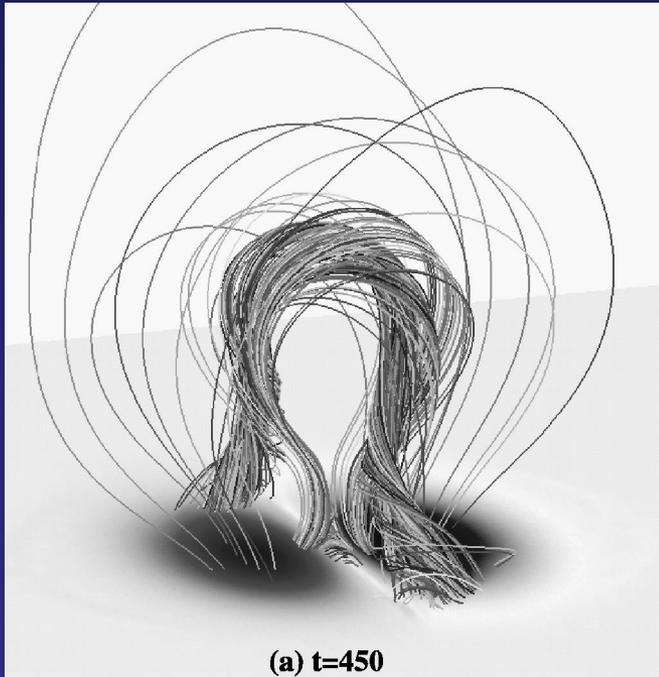




Sheared arcade
→ twisted rope

(Amari et al. 2000)





(Amari et al. 2000)

Unified flare model:

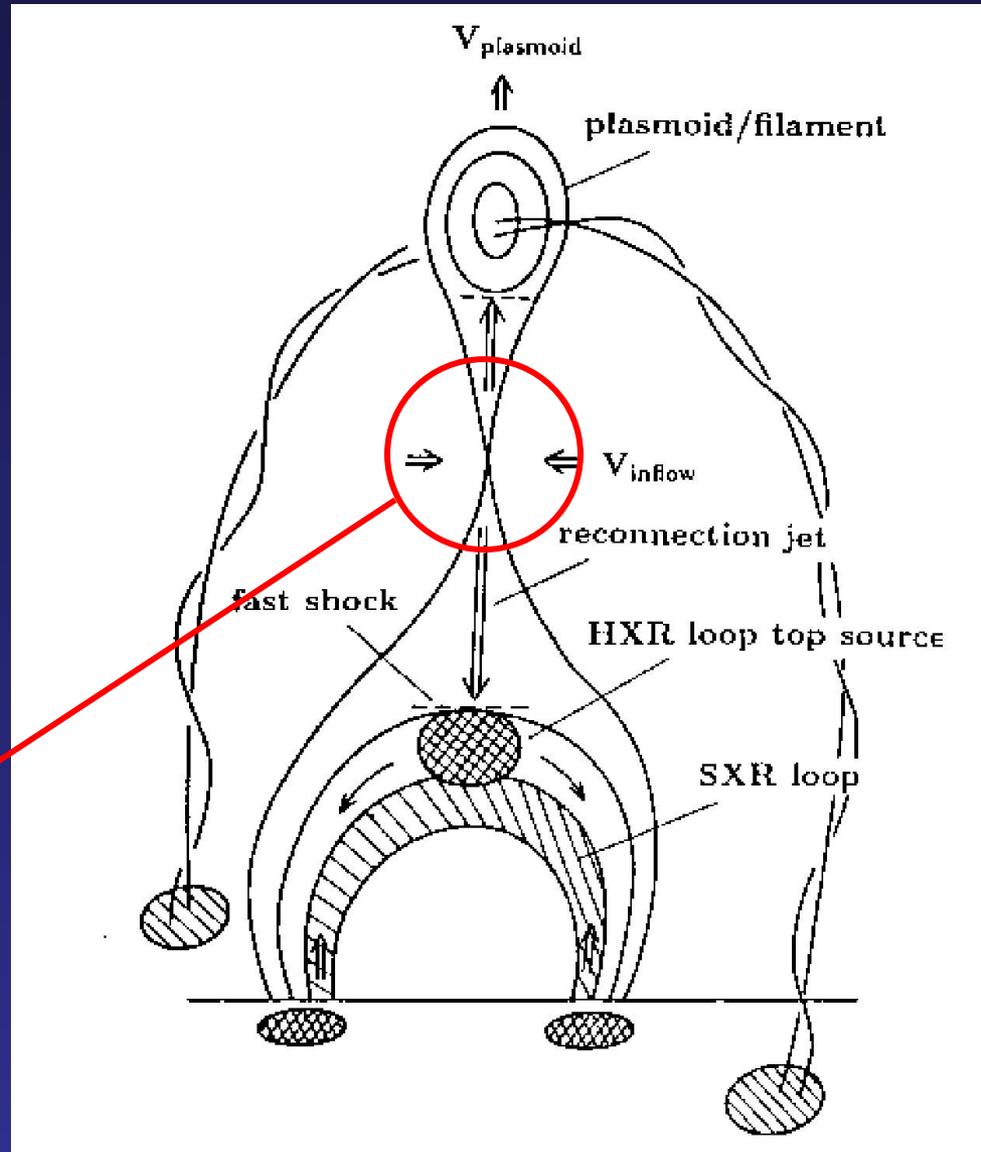
explains

- filament eruption
- mass ejection
- flare proper

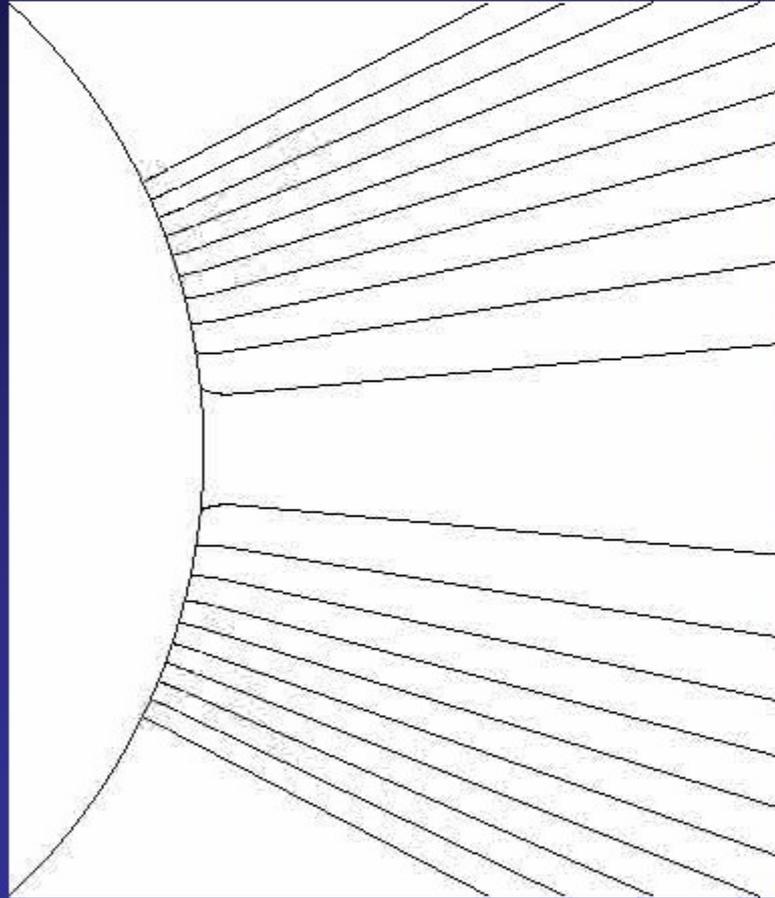
at once

place of action:

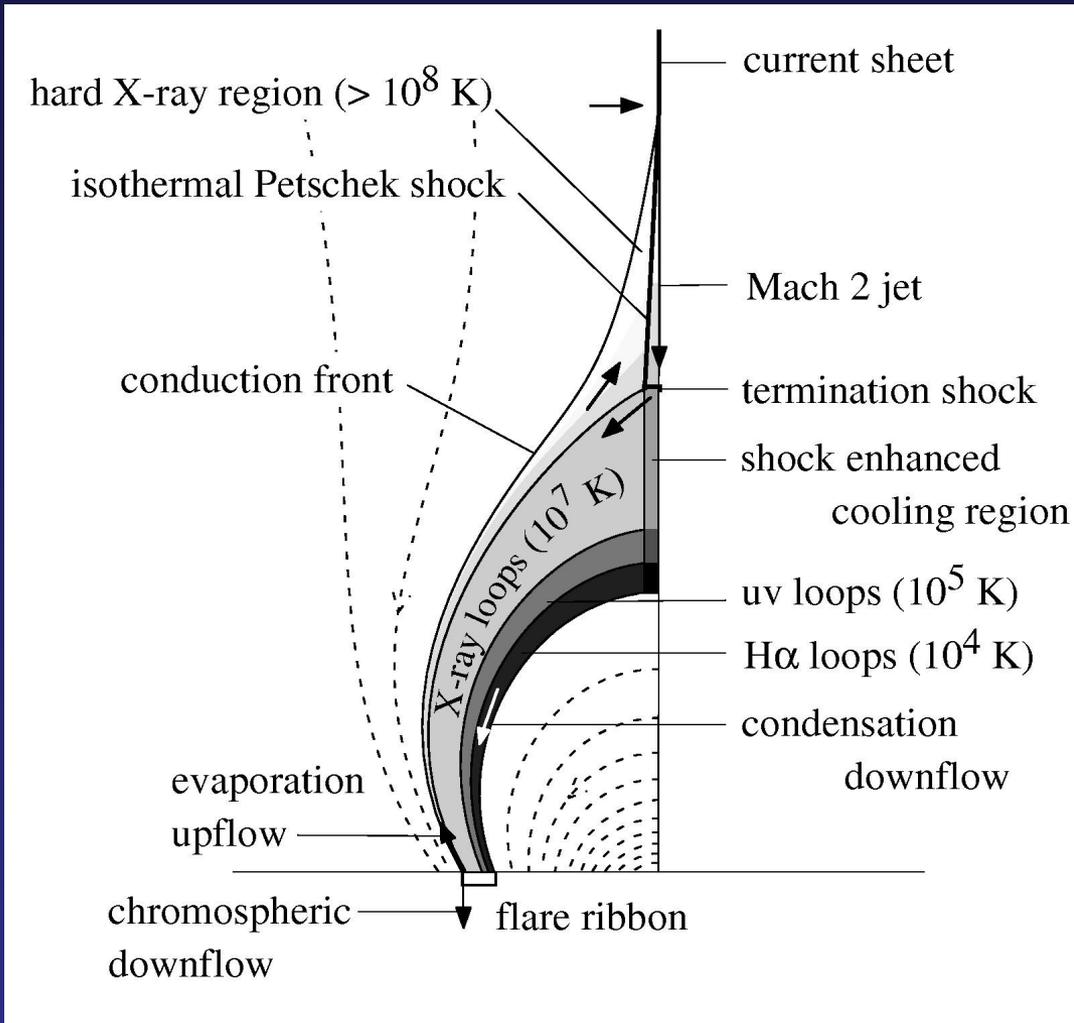
- heating
- shock formation
- particle acceleration



(Shibata 1999)



Cargese, 6 April
2006



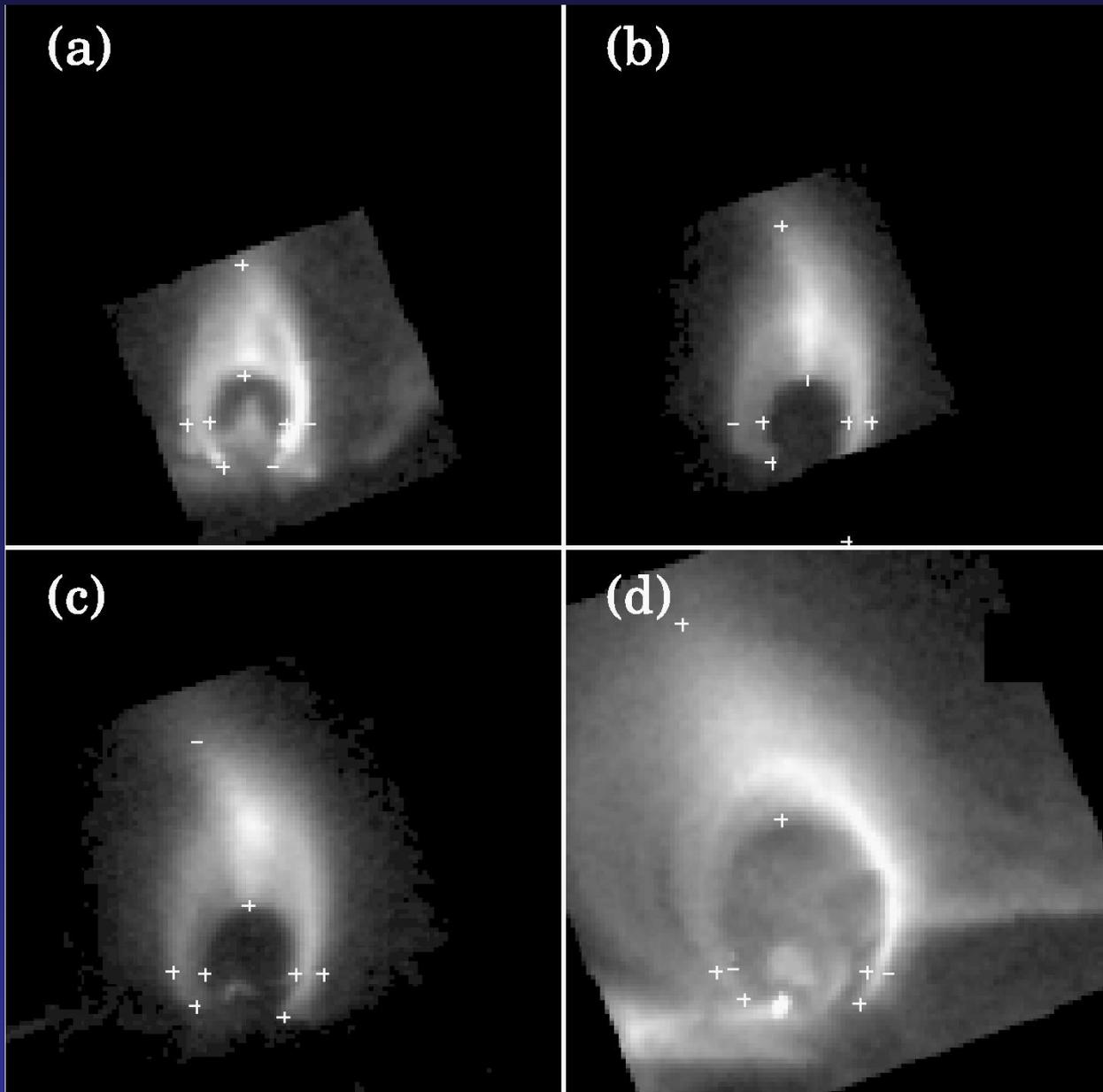
(Priest & Forbes 2002)

For the X-ray observer:
closed magnetic loops
heat up and evaporate
chromospheric material:

X-ray bright loops

Uppermost, new loops:
X-rays

lower loops:
cooling, H α

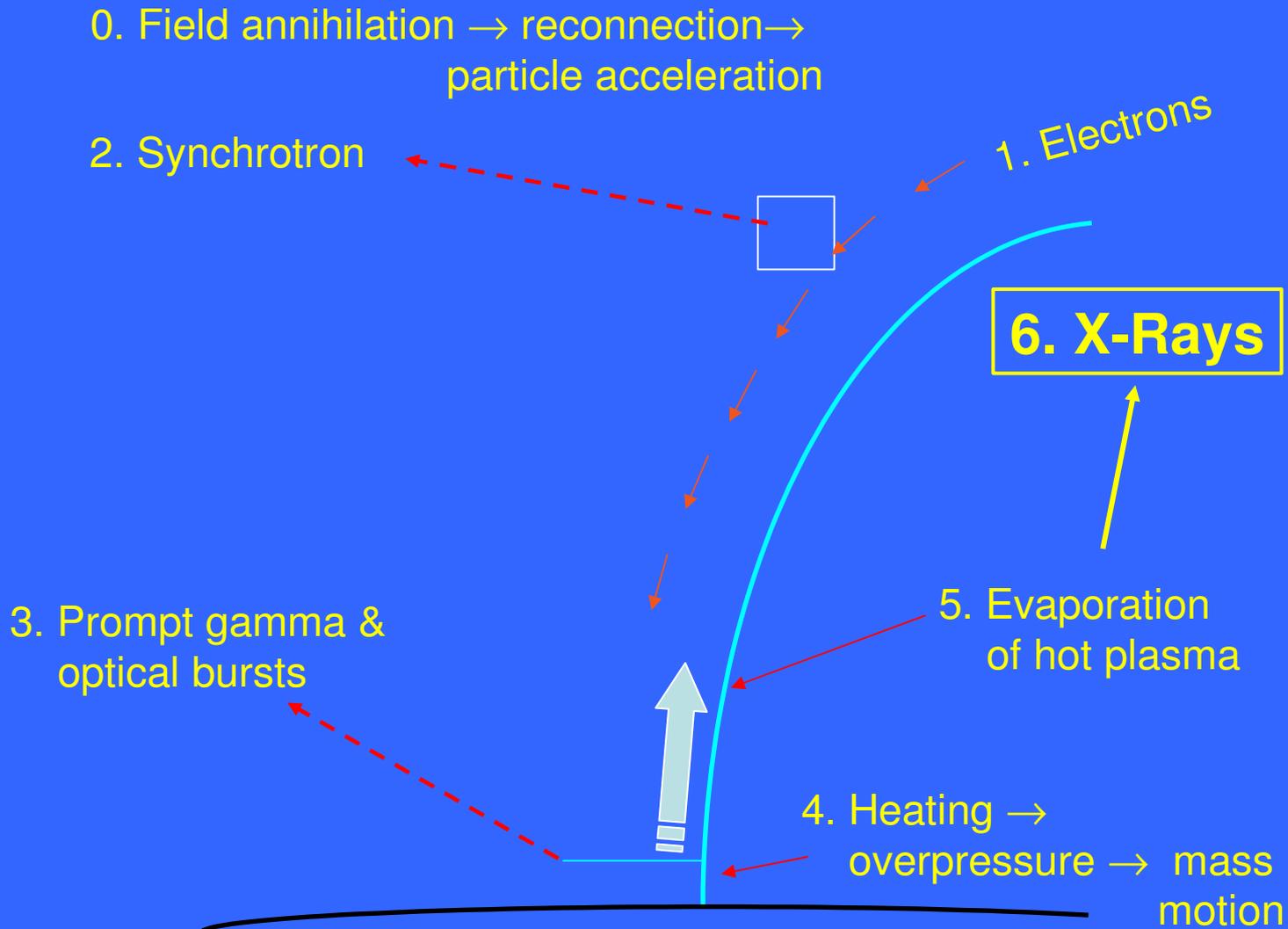


Growing X-ray
arcade (Yohkoh)

Cargese, 6 April
2006

(Forbes & Acton 1996)

Standard flare scenario after reconnection



approximation: radiative loss time \gg energy release time

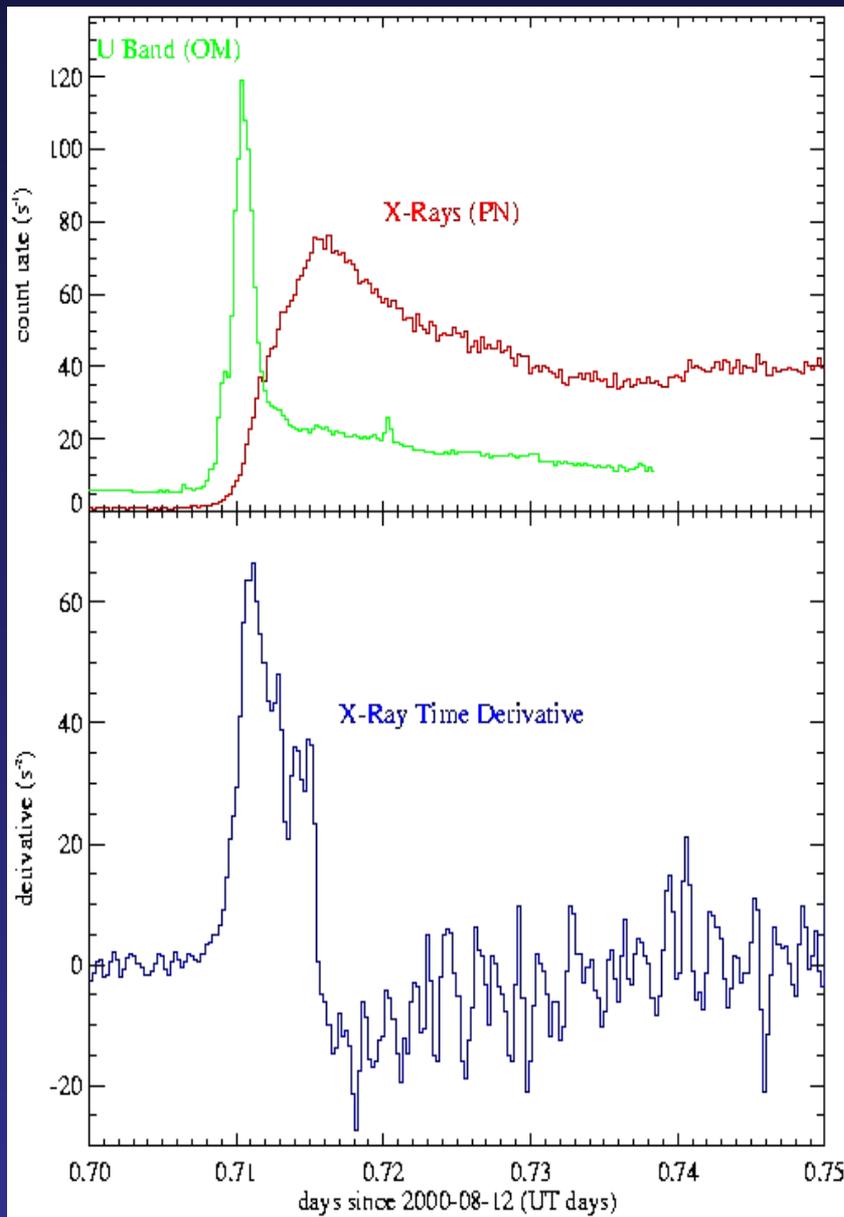
$$\frac{d}{dt}(3n_e kTV) \propto \text{electron flux} \propto L_R$$

$$\frac{d}{dt}L_X \propto L_R$$

(the proportionality between thermal energy content and radiative loss is a crude approximation)

Same for optical bursts:

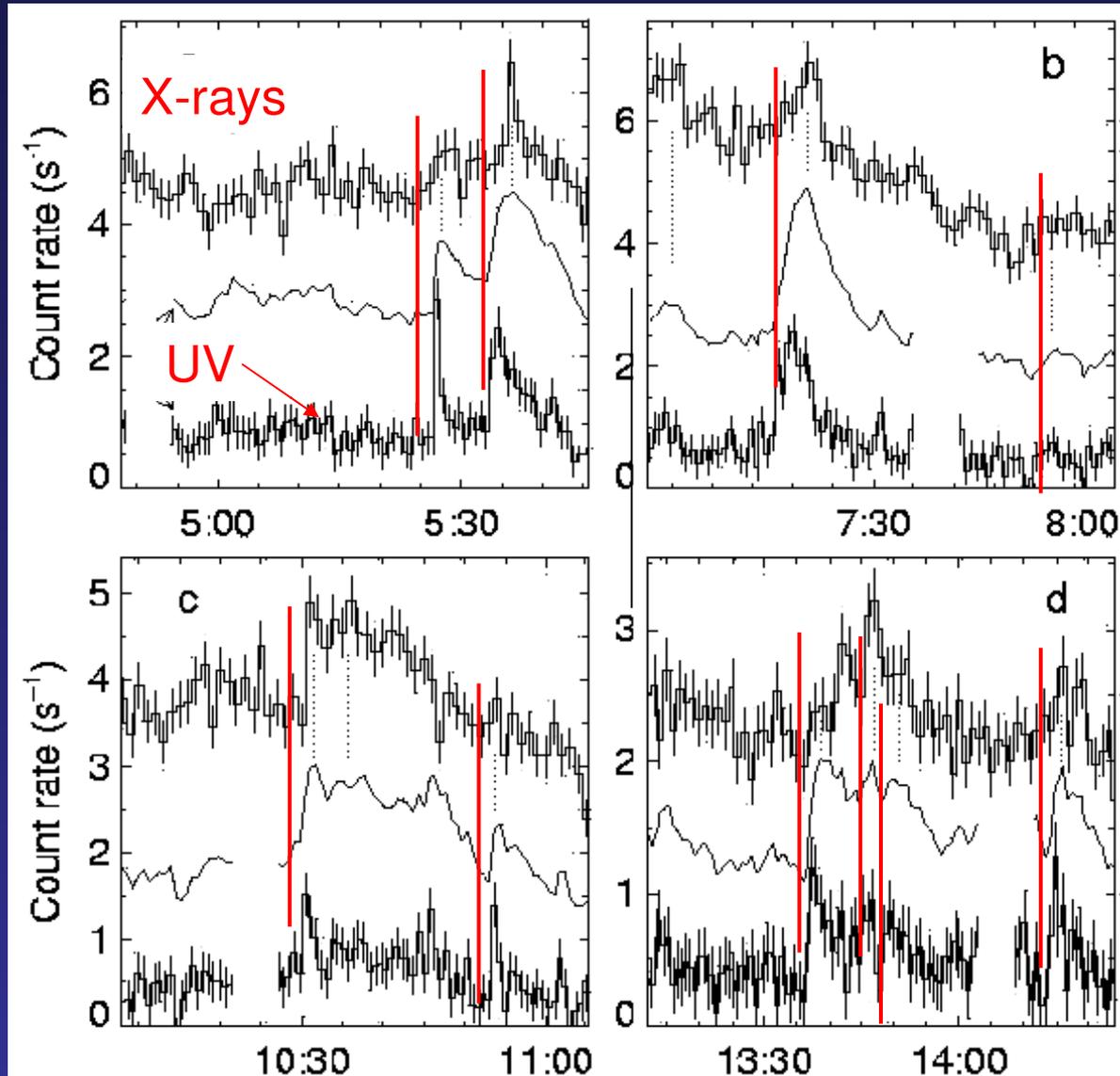
"Neupert Effect"



(Güdel et al. 2002)

Continuous Flaring

Smallest stellar flares seen in X-rays



Stochastic Heating

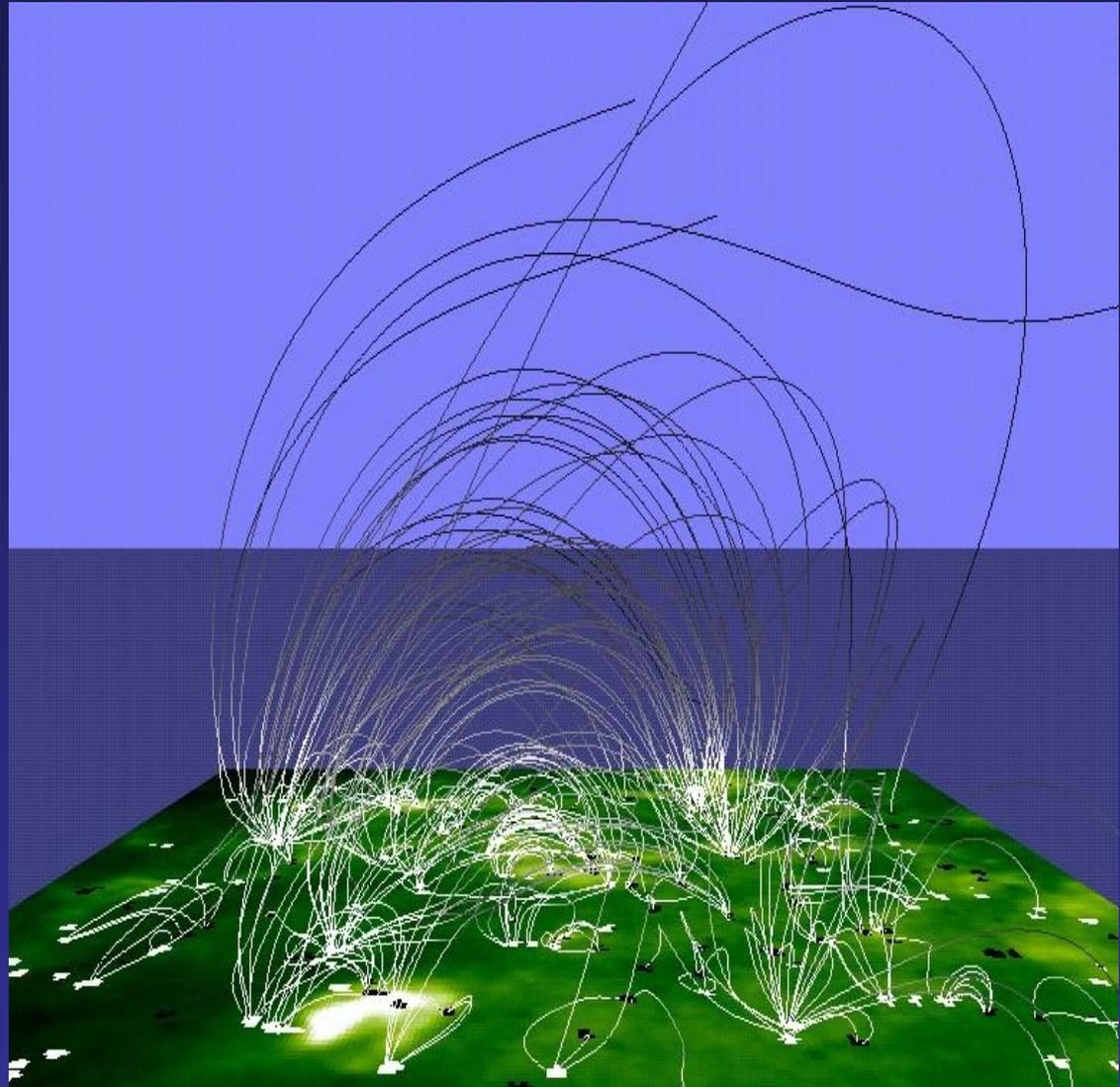
Tangential discontinuities
owing to footpoint motion



current sheets, reconnection

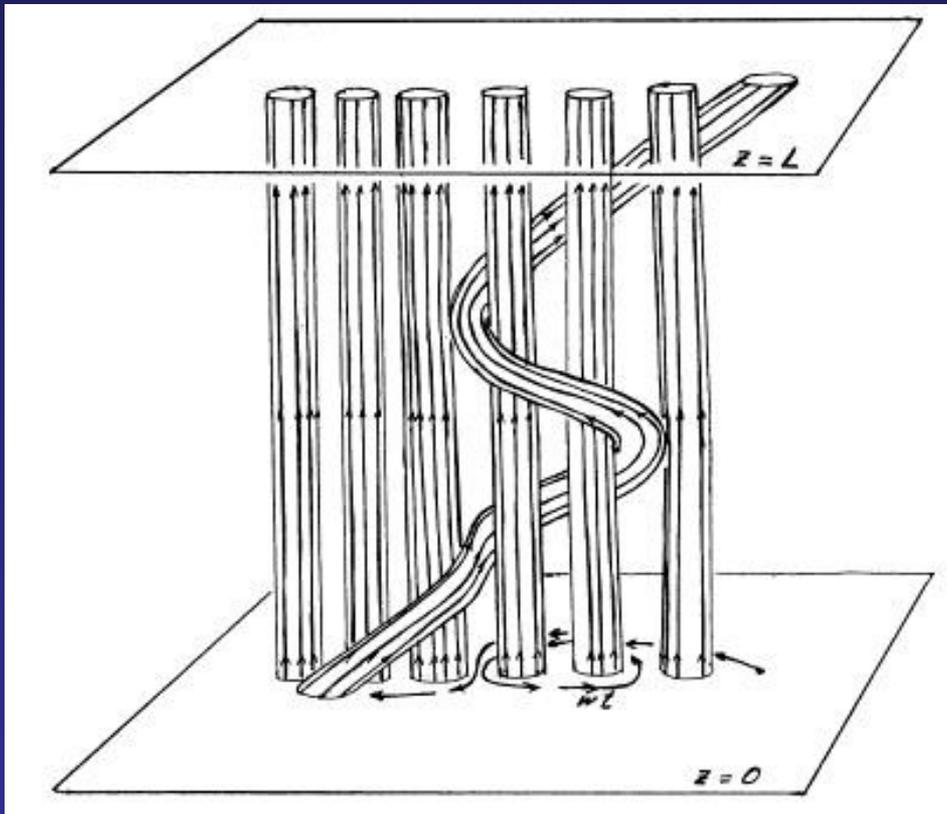


Stochastic energy release
(Parker 1988)



Conclusions for heating:

Tangled magnetic fields in random walk driven by footpoint motion produce current sheets in which magnetic fields reconnect:



Energy release of order
 $10^{24} - 10^{27}$ erg over
100 sec

(Parker 1983)

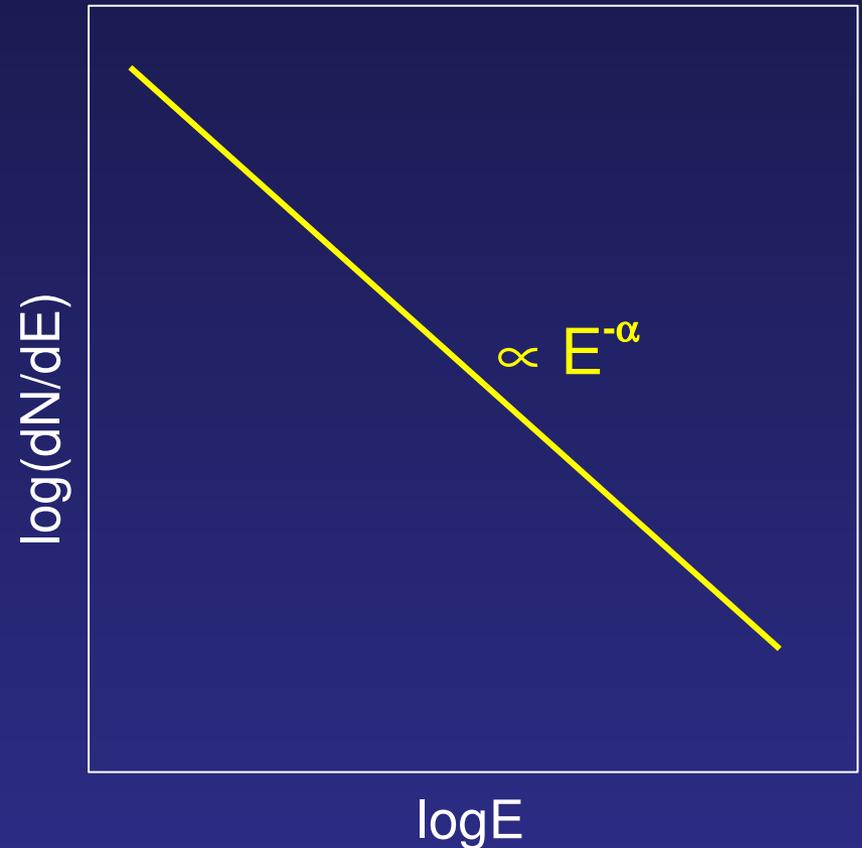
FLARE ENERGY DISTRIBUTIONS

$$dN/dE \propto E^{-\alpha}$$

E²

$$L_X \propto \int_{E_1}^{E_2} E dN/dE dE$$

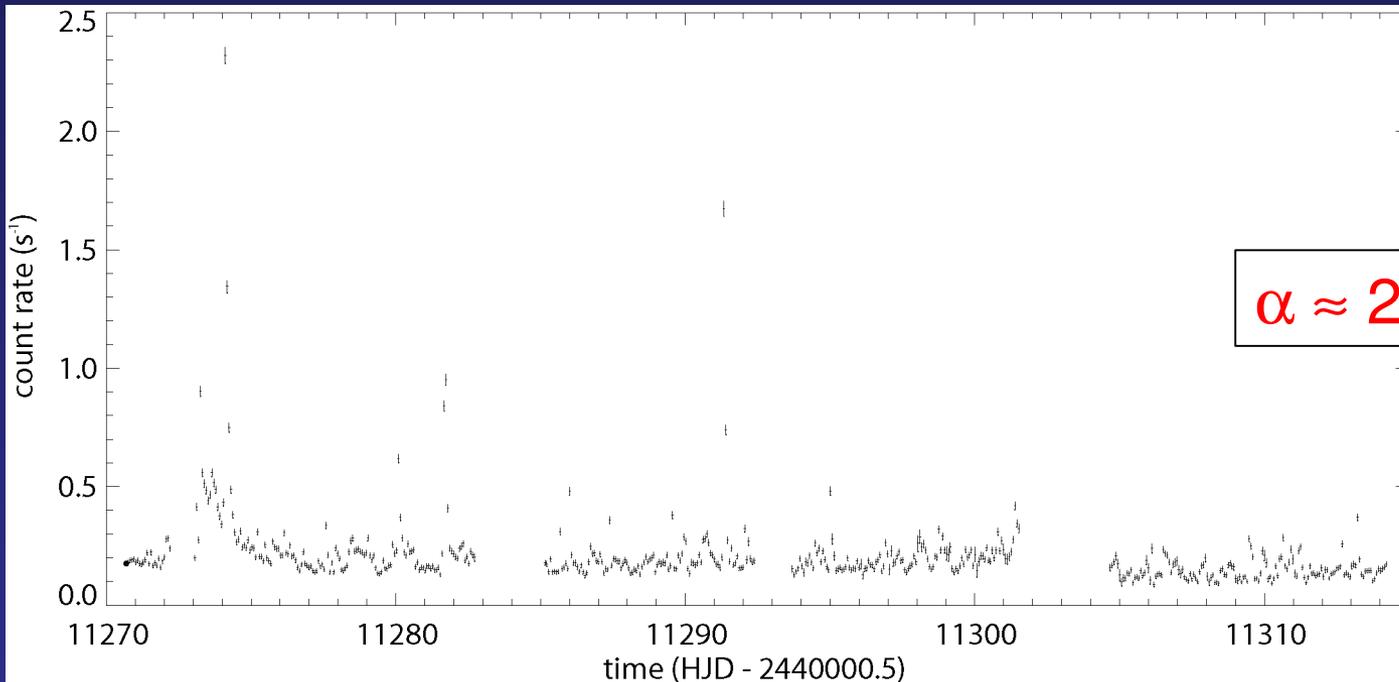
$\alpha \geq 2$: divergence for
 $E_1 \rightarrow 0$
("microflares")



In that case, all of the observed (quasi-steady) emission may be due to the superposition of small flares

Statistical tests of light curves show that
 $dN/dE \propto E^{-\alpha}$ implies $\alpha > 2$

(Audard et al. 1999, 2000, Güdel et al. 2003, Kashyap et al. 2002, Arzner & Güdel 2004)



44 days

(Güdel et al. 2003)

Flares distributed in energy:

$$dN/dE = E^{-\alpha}$$

Each flare decays exponentially
in T , EM , L_X :

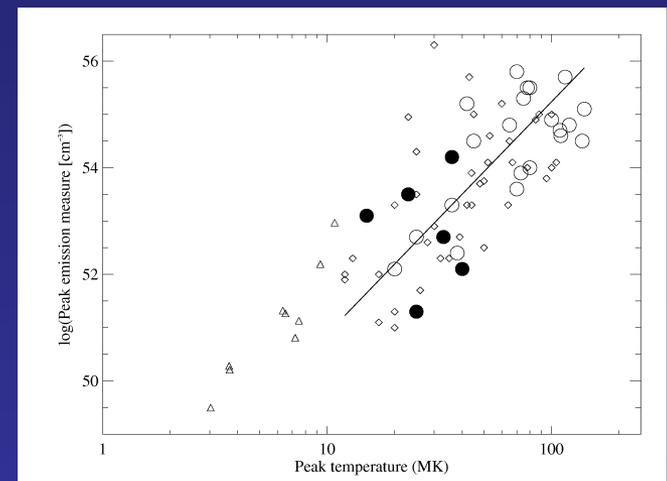
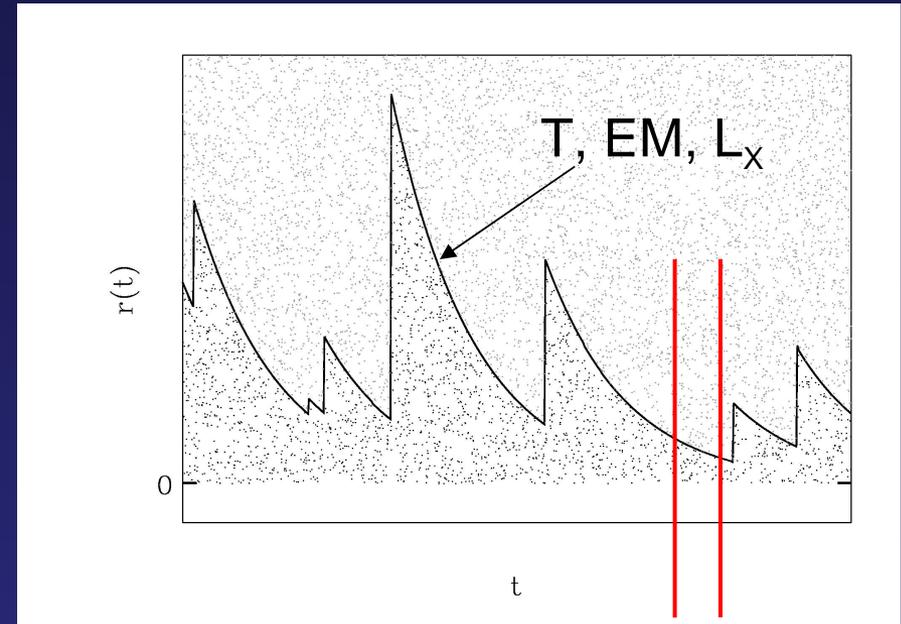
The peak T and EMs correlate:

$$EM_0 = aT_0^b \quad [\text{cm}^{-3}] \quad (b = 4.3)$$

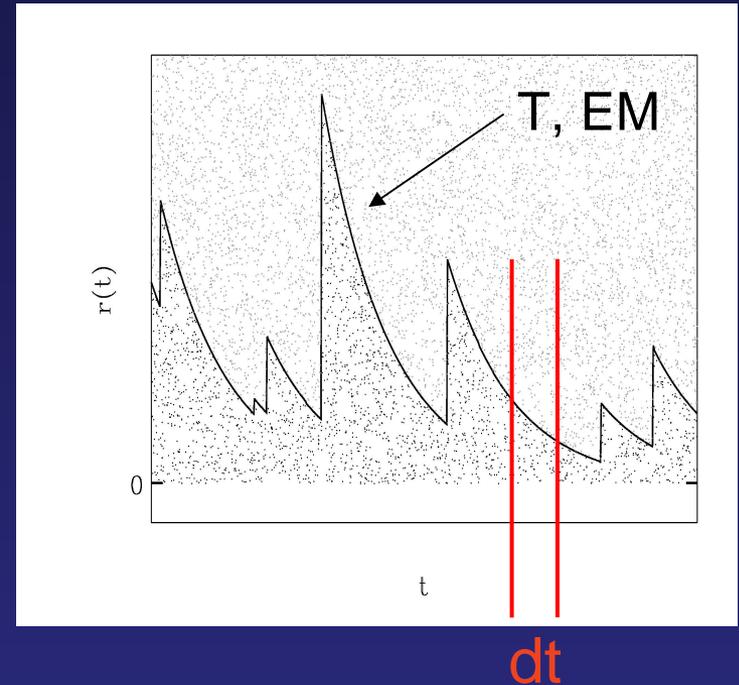
T and n_e decay like $T \propto n^\zeta \quad \zeta \approx 0.5 - 2$

Radiation

$$L_X \approx EM \Lambda(T) = f EM T^{-\phi}$$

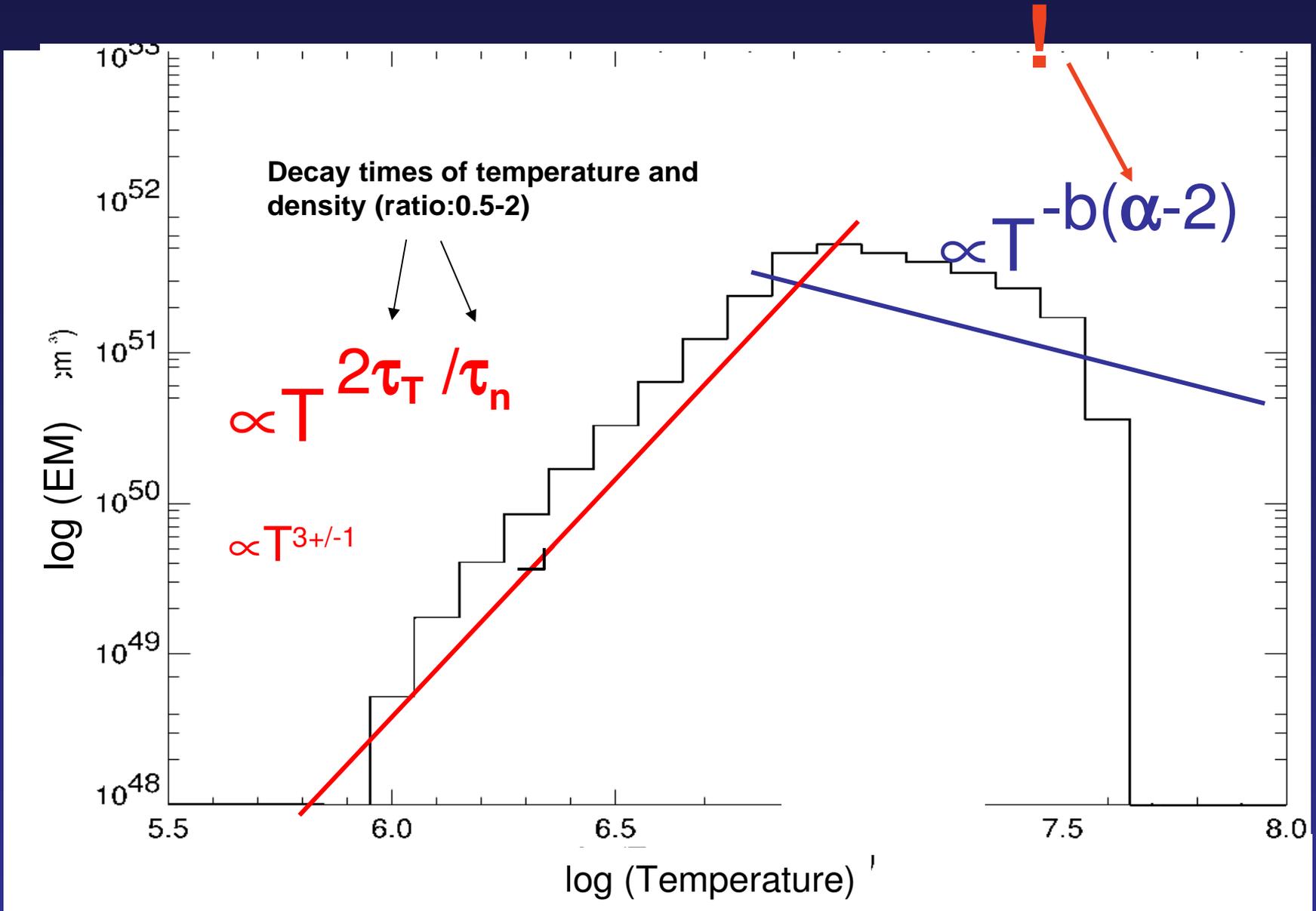


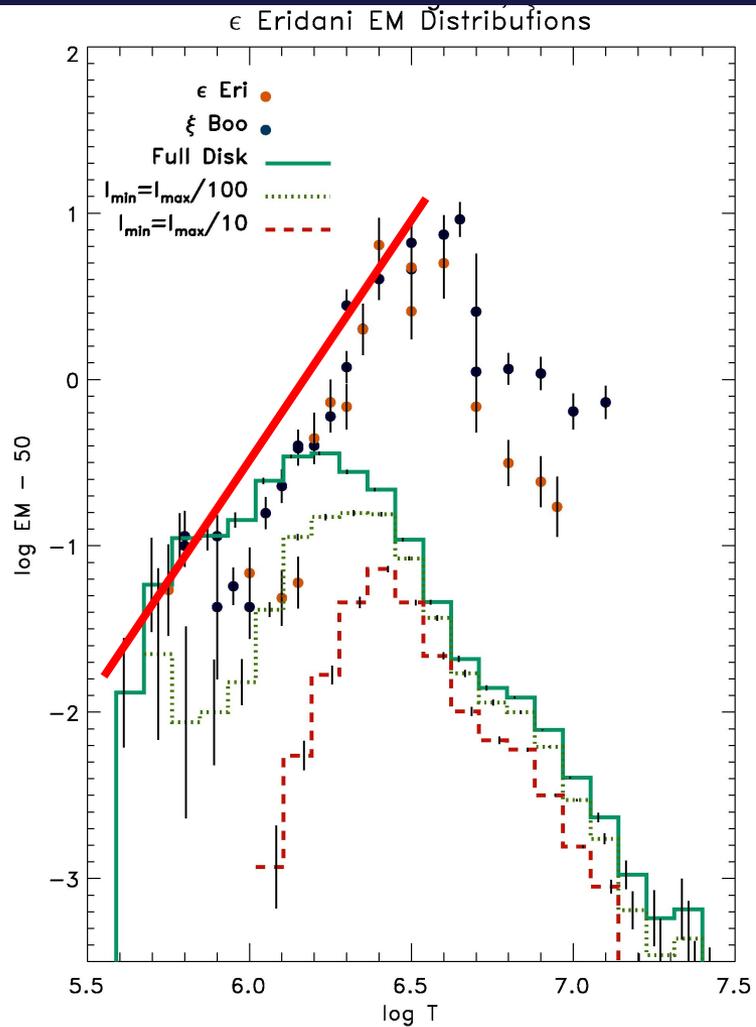
and integrate over flare evolution and
the distribution of flares



$$Q(T) \propto \begin{cases} T^2/\zeta & \text{for } T < T_m \\ T^{-(b-\phi)(\alpha-2\beta)/(1-\beta)+2b-\phi} & \text{for } T > T_m \end{cases}$$

(Güdel et al. 2003)





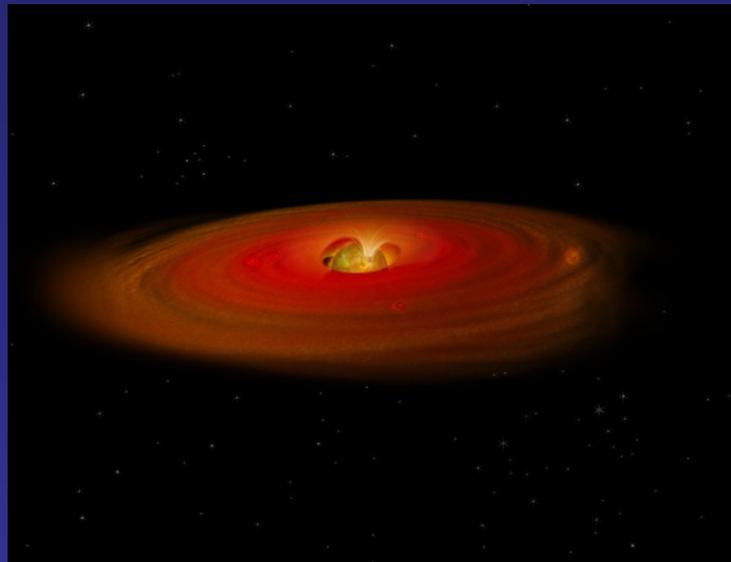
Power-law DEMs
measured in stellar coronae
are steep on low-T side
(slopes of 2-4)

(Drake et al. 2000)

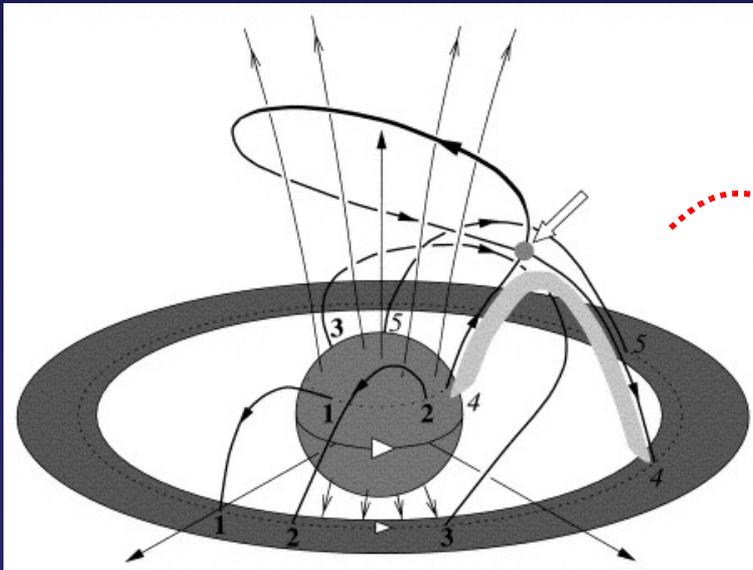
Toward Pre-Main Sequence Stars

Low-mass stars < 10 Myr:
Accretion disks/flows, winds, jets, outflows, molecular clouds
may matter

Classical T Tau stars: active accretion from disk, microjets

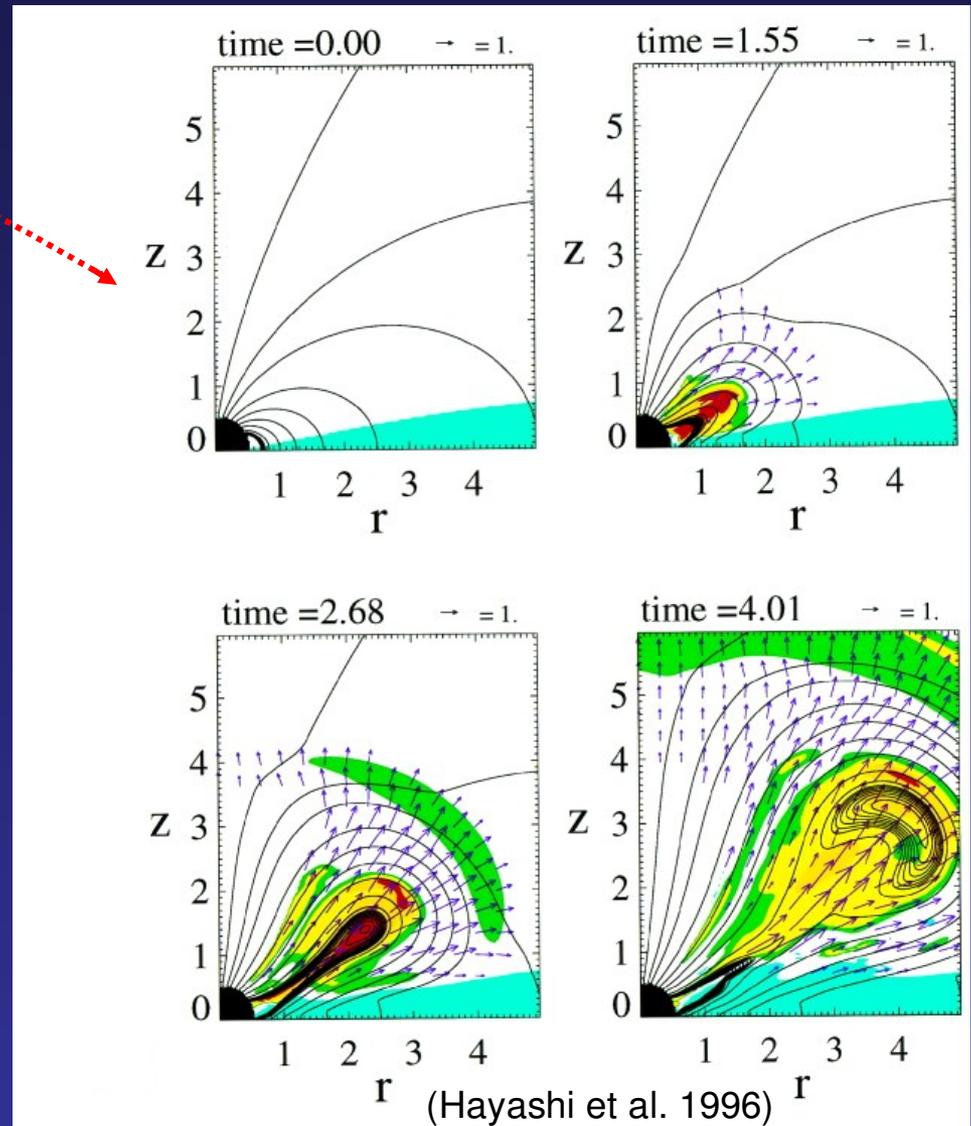


Reconnection, Heating, and Jet Formation



Wind-up of magnetic field lines
(Montmerle et al. 2000):

- Antiparallel magnetic fields
- Heating and reconnection
- Ejection of hot plasma clouds
- Jets? Outflow due to accretion

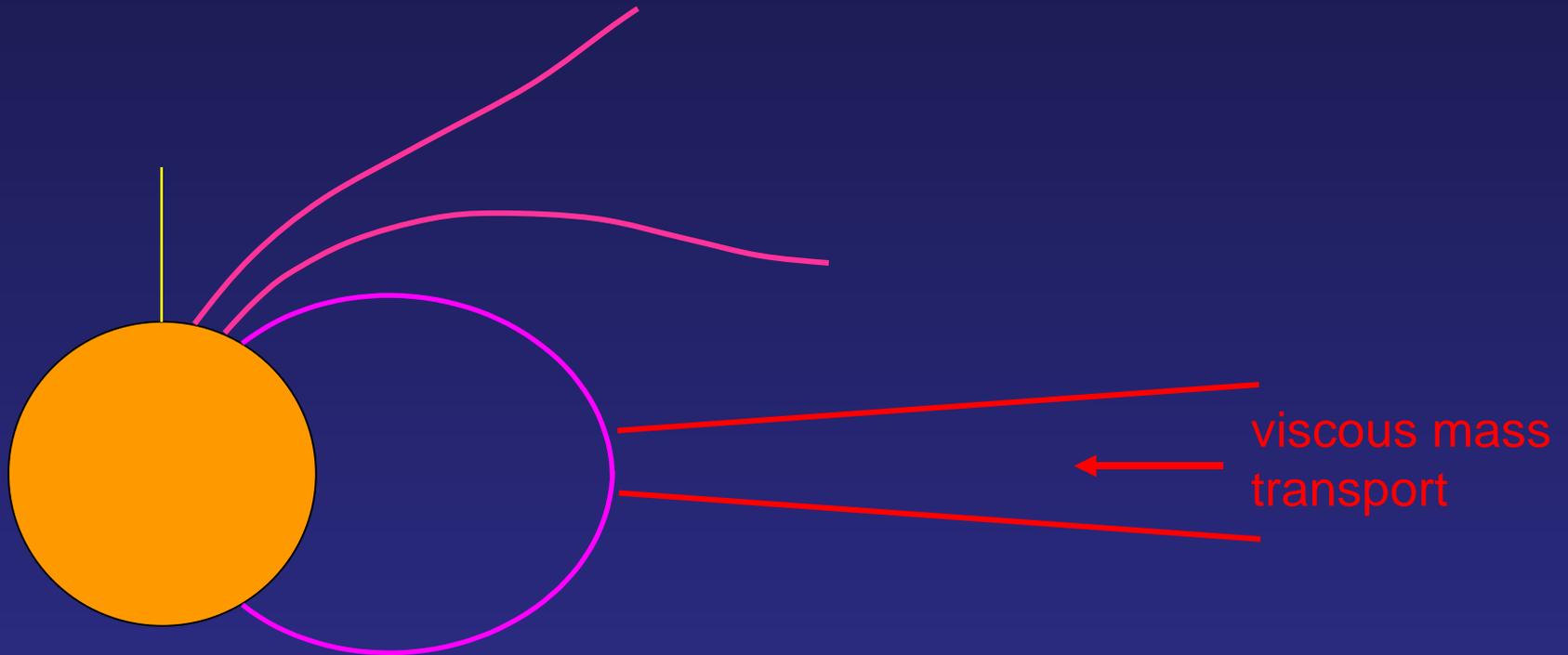


Plasmoid ejection may be
the origin of jets:

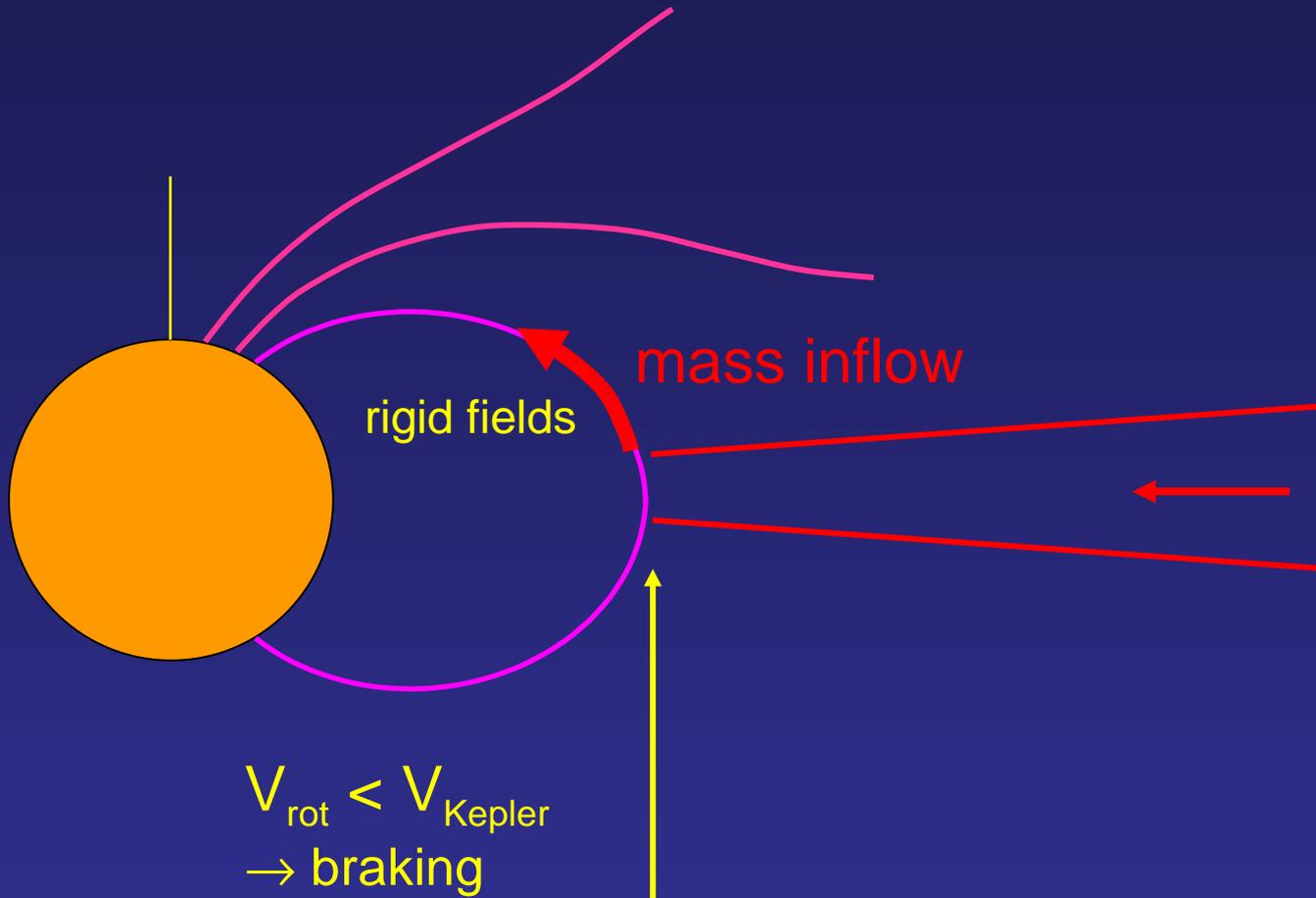
typical outflow velocities

$\approx 300 \text{ km/s}$

Magnetic fields and accretion onto the star



Magnetic fields and accretion onto the star: Magnetic funneling

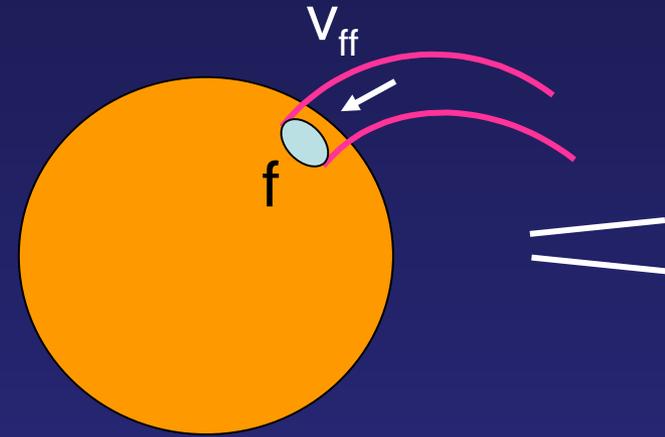


Magnetic accretion onto stars:

$$T_s = \frac{3}{16k} \mu m_p v^2$$

$$v \approx v_{\text{ff}} = \left(\frac{2GM}{R} \right)^{1/2}$$

$$\dot{M} = 4\pi R^2 f \cdot m_p n \cdot v_{\text{ff}}$$

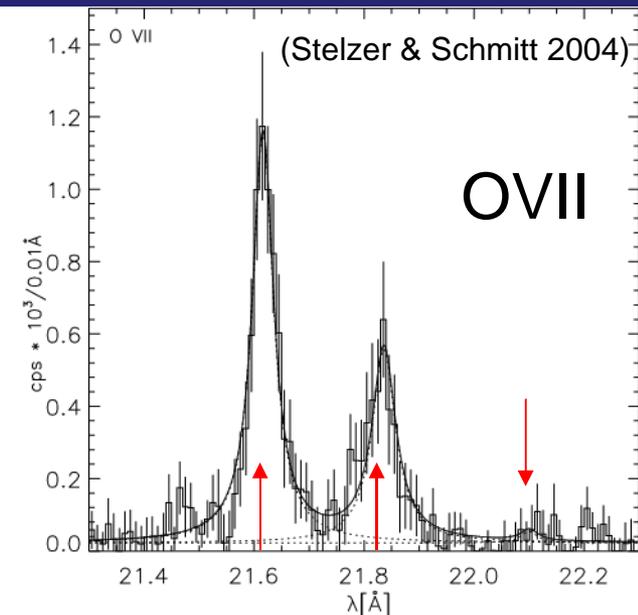
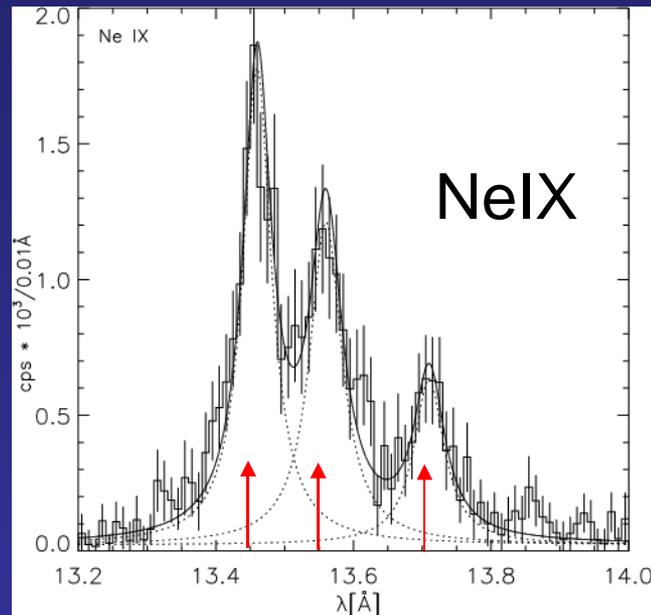
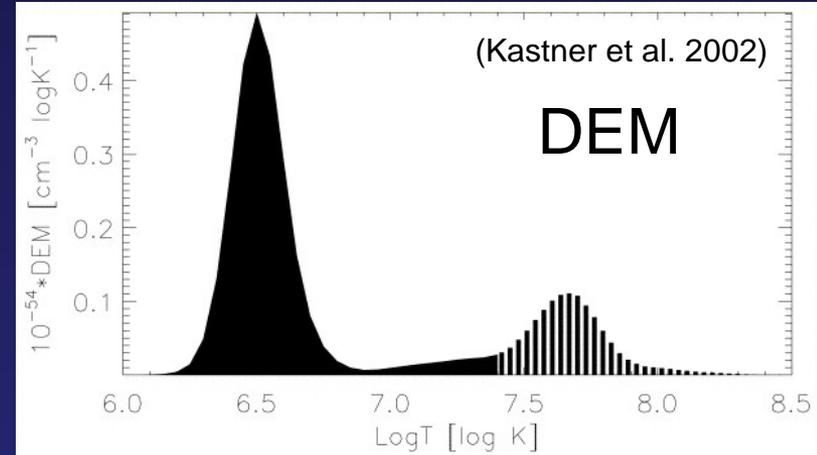


→ T a few MK

→ $n_e \approx 10^{12}-10^{14} \text{ cm}^{-3}$

X-ray spectroscopy of CTTS: TW Hya

- DEM peaks at 3×10^6 K
- high densities: 10^{13} cm $^{-3}$



Summary

Magnetically active stars as ideal sources to test coronal heating models, in particular flare-related models. Much of the "basic physics" is really studied in the solar corona.

- Basic building blocks of a stellar corona are closed magnetic "loops" filled with 1-100 MK plasma
- Principal energy release at large heights due to reconnecting fields, inducing particle acceleration and heating
- Magnetic structures may not be static: time-dependent heating + flows
- Emission measure distributions are compatible with stochastic flaring
- Flare statistics support flare-heating models
- Alternative X-ray mechanisms in accretion and jets being studied

END